

# Amplifier Noise

INEL 5207 - ECE Dept. UPRM

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# Objectives

- ◆ Estimate expected amount of output noise
- ◆ Determine minimum usable signal level
- ◆ Gain insight into possible improvements

# Basic Concepts

- ♦ Many types of noise
  - ♦ interference, or external, noise
  - ♦ d.c. offsets are a form of noise
  - ♦ we will study **internal or inherent noise**

- ♦ RMS value over averaging interval T:

$$X_n = \frac{1}{T} \sqrt{\int_0^T x_n^2(t) dt}$$

- ♦  $X_n^2$  is the *mean square value* of noise
- ♦  $x$  represents current  $i$  or voltage  $e$
- ♦ We will deal with multiple sources of noise
- ♦ Different noise sources are added as vectors

$$X_n = \sqrt{X_{n1}^2 + X_{n2}^2}$$

# Frequency Domain

- ◆ Noise RMS: computed in the frequency domain
- ◆ The *noise power density* is normally specified

$$x_n^2(f) = \frac{dX_n^2}{df}$$

- ◆ From the power density the rms value is found

$$X_n = \sqrt{\int_{f_L}^{f_H} x_n^2(f) df}$$

- ◆ replace  $X$  with  $I$  for current,  $V$  for voltage

# White & $1/f$ Noise

- ♦ White: uniform spectral density

$$X_n = x_{nw} \sqrt{f_H - f_L}$$

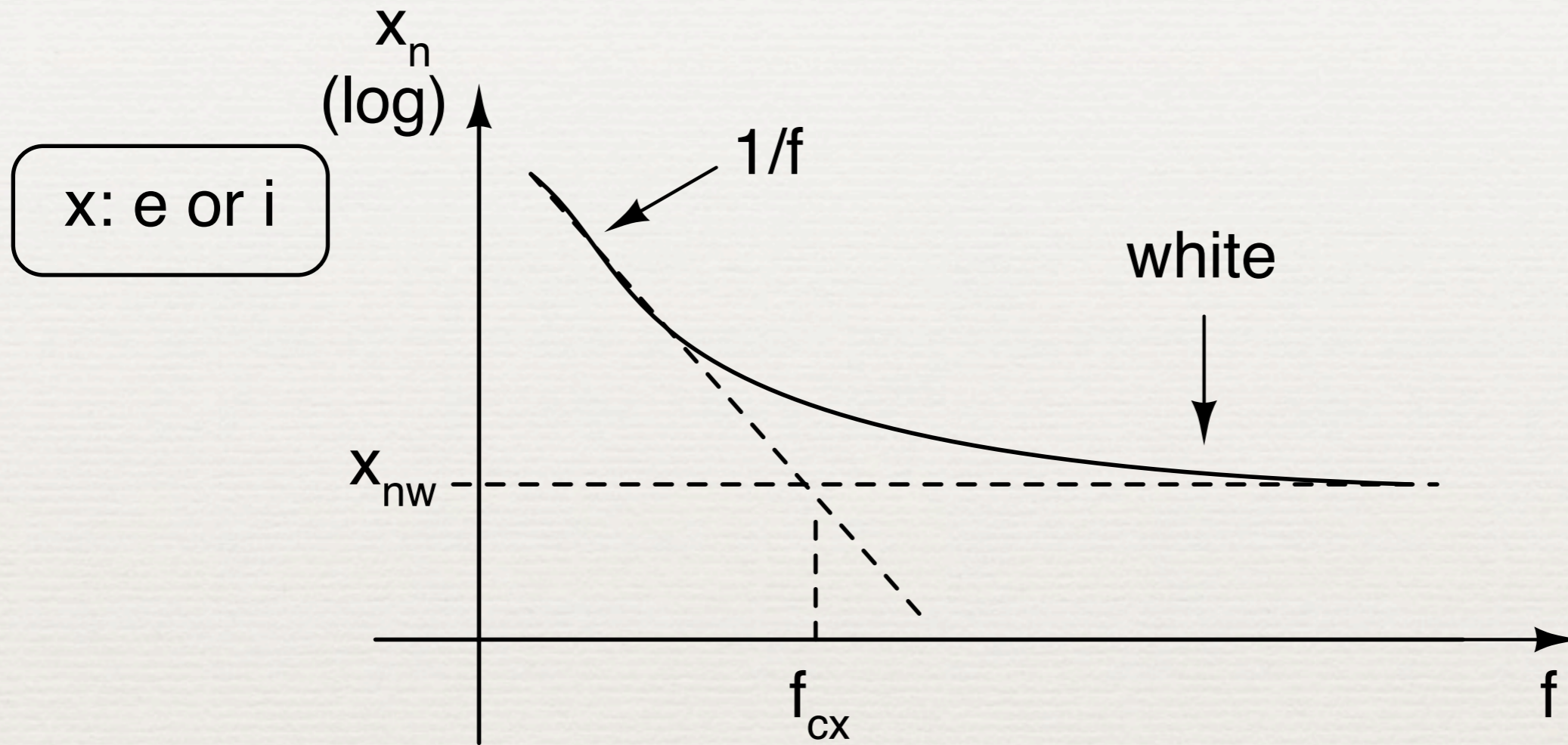
- ♦ white-noise power is proportional to BW

- ♦  $1/f$  noise: varies with reciprocal of  $f$

$$x_n = K/\sqrt{f} \rightarrow X_n = K \sqrt{\ln(f_H/f_L)}$$

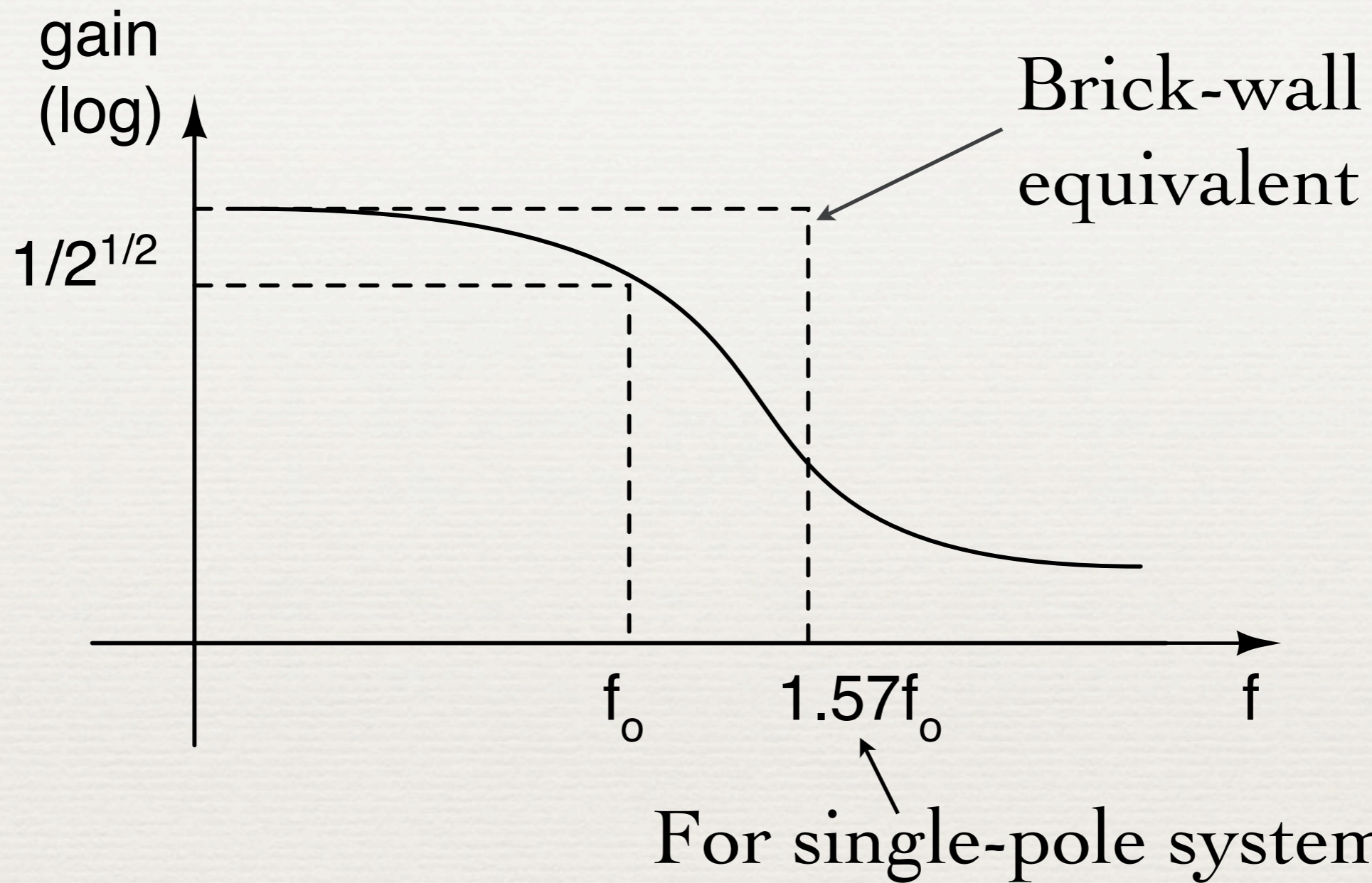
- ♦  $1/f$  - noise power is proportional to # of decades or octaves

# IC noise - mixture of white+1/f



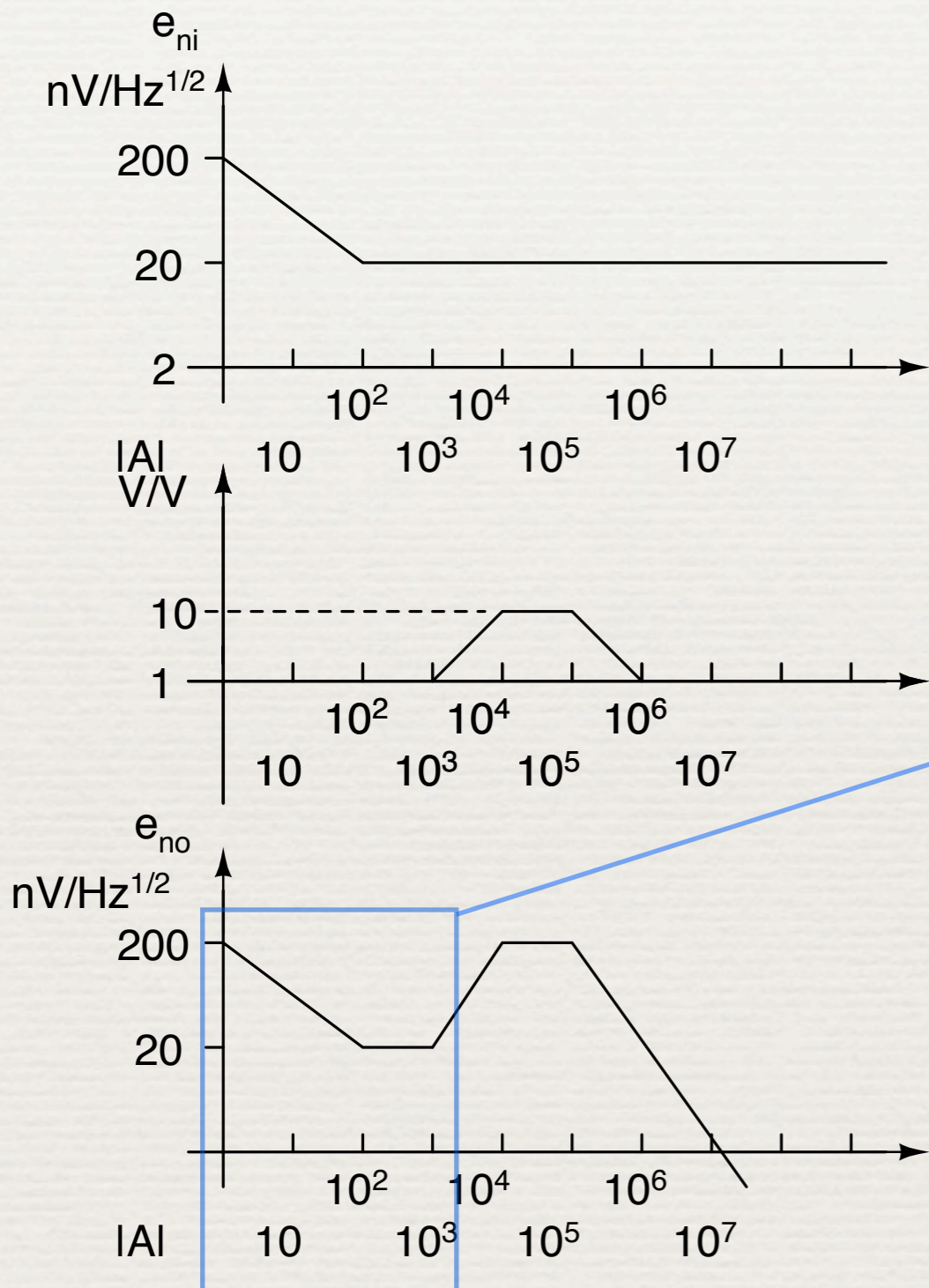
$$x_n^2 = x_{nw}^2 \left( \frac{f_{cx}}{f} + 1 \right) \rightarrow X_n = x_{nw} \sqrt{f_{cx} \ln(f_H/f_L) + f_H - f_L}$$

- ♦ Normally noise is described by specifying  $e_{nw}$  and  $f_{ce}$  (voltage) or  $i_{nw}$  and  $f_{ci}$  (current)
- ♦ Source of noise appear in different places, and equivalent input noise sources are found
- ♦ Input sources are filtered by amplifier to produce output noise
- ♦ To simplify calculations, actual magnitude response is replaced by a *Brick-wall equivalent*



Noise-equivalent bandwidth:  $1.57f_0$  for above case

# Example 7.3 Piece-wise noise integration



1 Hz to 1kHz:

$$E_n = e_{nw} \sqrt{f_{ce} \ln(f_H/f_L) + f_H - f_L}$$

with

$$e_{nw} = 20 \text{ nV} / \sqrt{\text{Hz}}$$

$$f_{ce} = 100 \text{ Hz} \quad f_L = 1 \text{ Hz}$$

and

$$f_H = 1 \text{ kHz}$$

The result is  $E_{no1} = 0.822 \mu\text{V}$ .

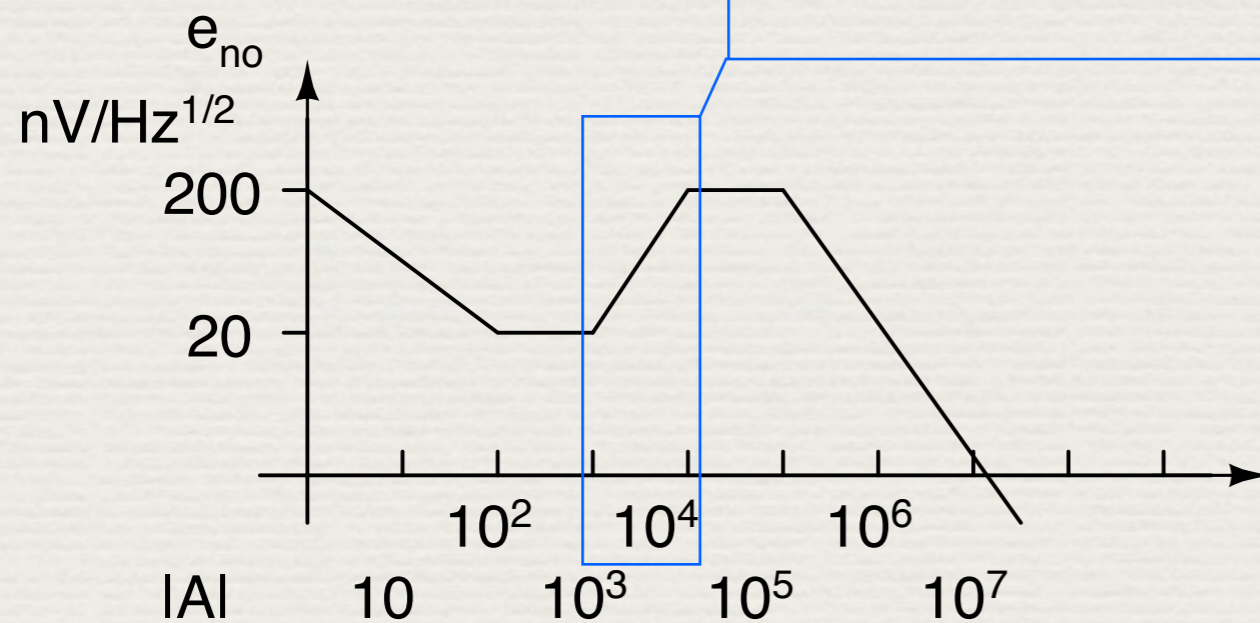
From 1kHz to 10kHz,  
 $e_{no}$  increases with  $f$  at a rate of  
 1dec/dec.

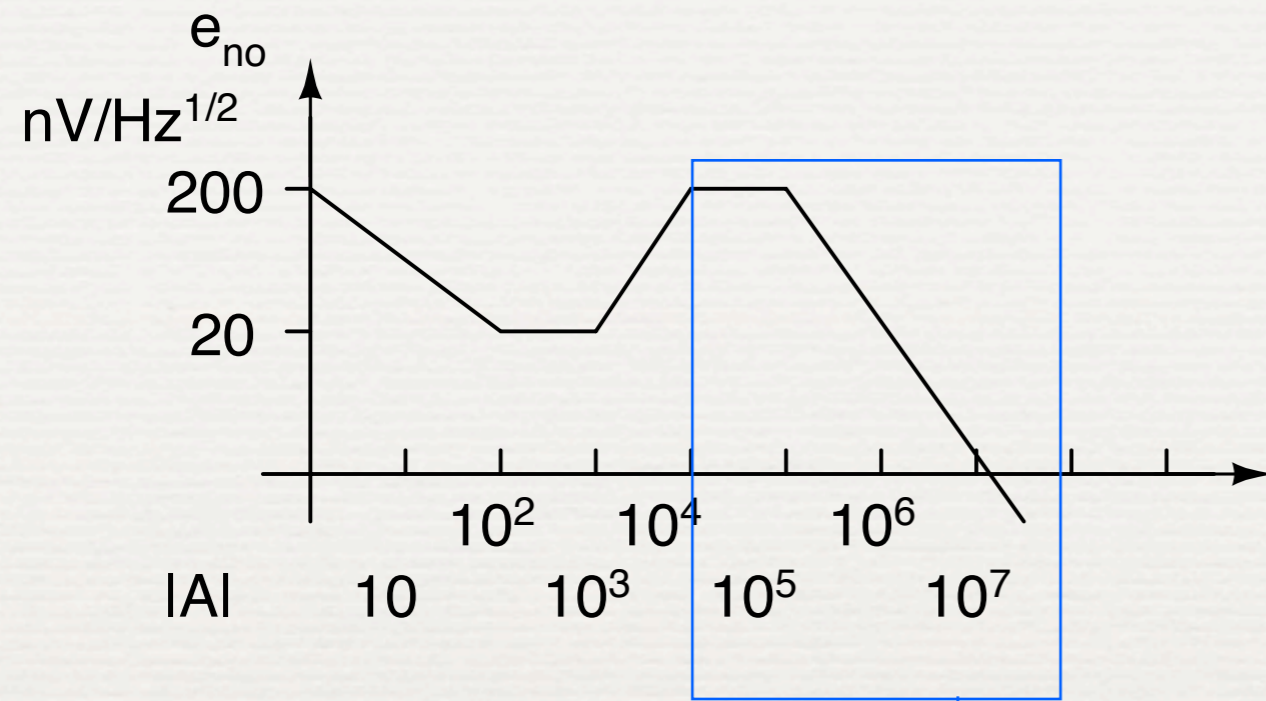
So let

$$e_{no}(f) = \left(20nV/\sqrt{Hz}\right) \times (f/10^3) = 2 \times 10^{-11} f$$

and

$$E_{no2} = 2 \times 10^{-11} \sqrt{\int_{10^3}^{10^4} f^2 df} = 11.5 \mu V$$





For  $f > 10^4 \text{ Hz}$ , we have white noise with  $e_{nw} = 200 \text{ nV}/\sqrt{\text{Hz}}$  going through a low-pass filter with corner frequency  $f_o = 100 \text{ kHz}$ . Using

$$E_{no3} = e_{nw} \sqrt{1.57 f_o}$$

$$E_{no3} = (200 \text{ nV}/\sqrt{\text{Hz}}) \times \sqrt{1.57 \times 10^5 - 10^4} =$$

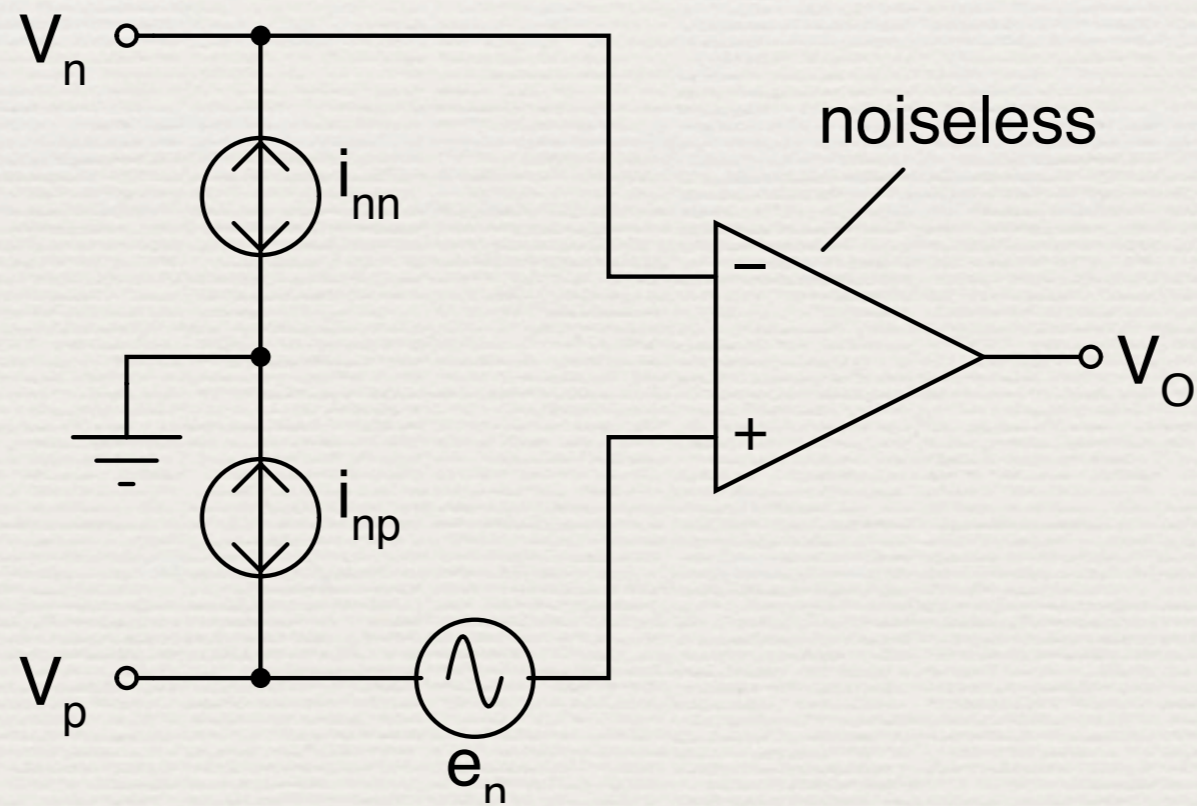
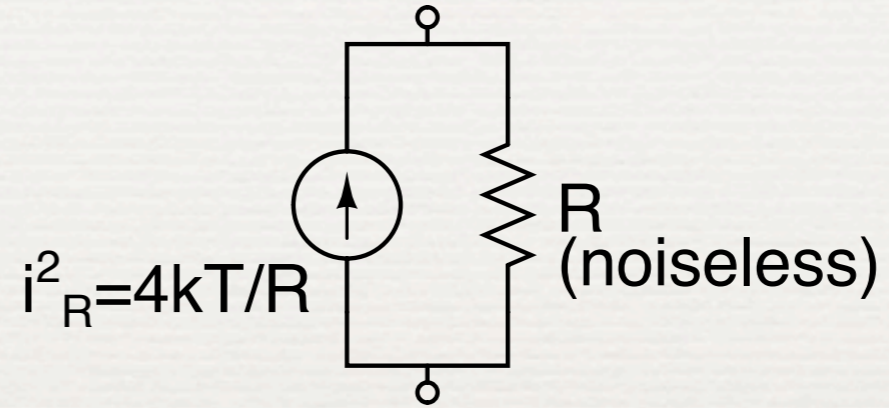
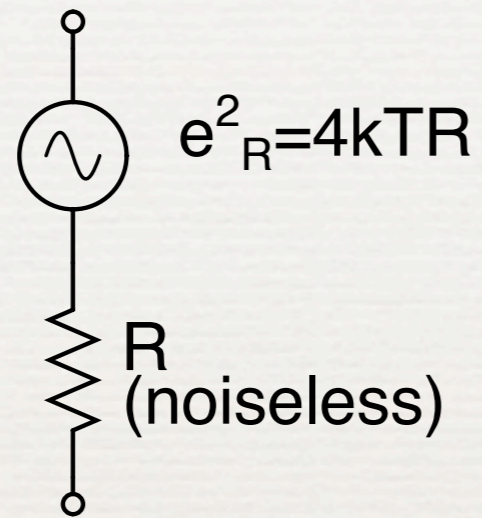
The total is the root of the sum of the square of the three components

$$E_{no} = \sqrt{E_{no1}^2 + E_{no2}^2 + E_{no3}^2} = 77.5\mu V$$

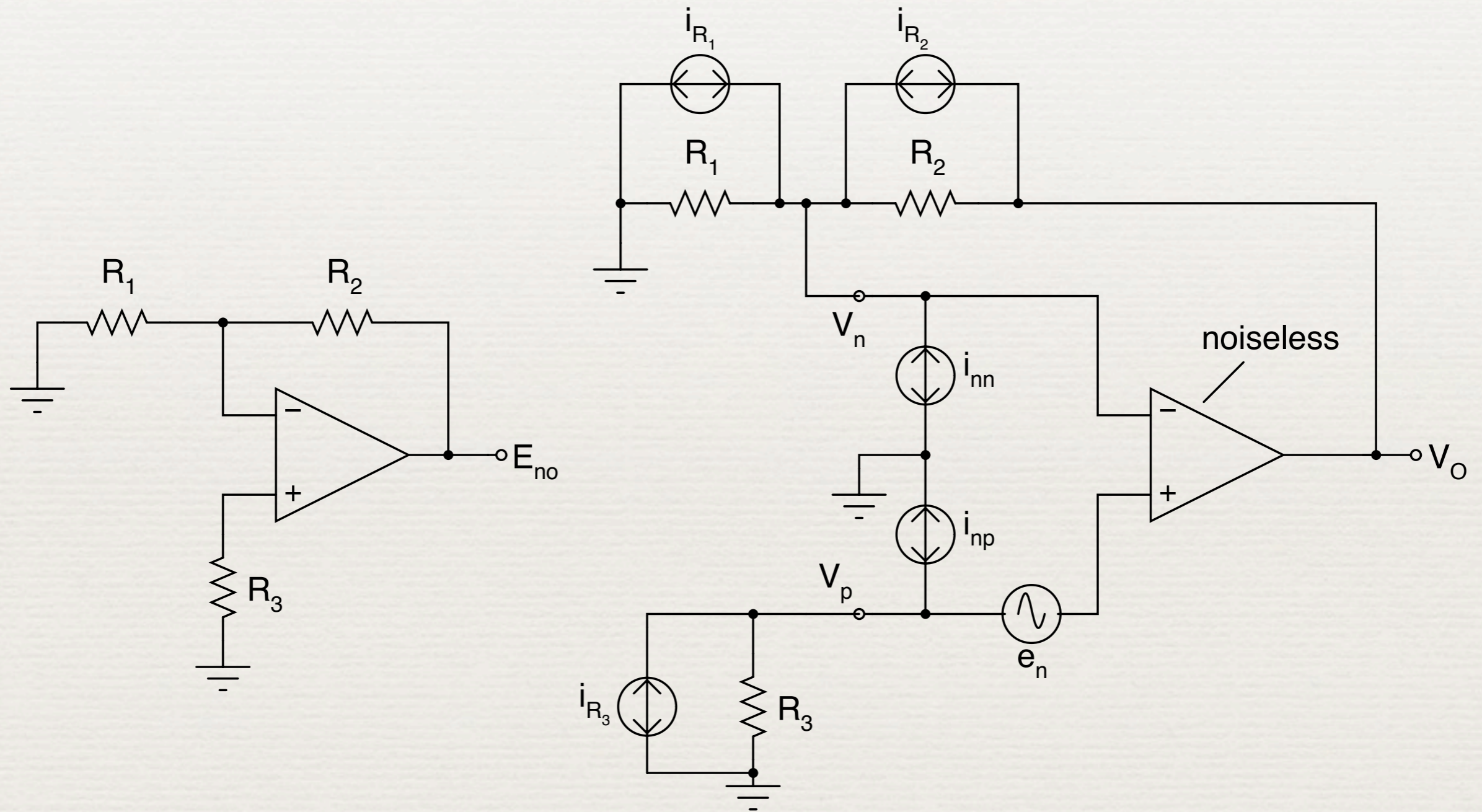
## **Pink-noise tangent principle**

Lower a line with -0.5 dec/dec slope until it becomes tangent to the noise curve. The main contribution to the output noise will come from the portion of the noise curve that is in the vicinity of the tangent point.

# Sources of noise



# Example 7.7



Use superposition to obtain:

$$e_{ni}^2 = e_n^2 + i_{np}^2 R_3^2 + i_{R_3}^2 R_3^2 + (i_{nn}^2 + i_{R_1}^2 + i_{R_2}^2) (R_1 \parallel R_2)^2$$

Using  $i_R^2 = \frac{4kT}{R}$ ,

$$\begin{aligned} e_{ni}^2 &= e_n^2 + i_{np}^2 R_3^2 + 4kT R_3 + \left( i_{nn}^2 + \frac{4kT}{R_1} + \frac{4kT}{R_2} \right) (R_1 \parallel R_2)^2 \\ &= e_n^2 + i_{np}^2 R_3^2 + 4kT R_3 + i_{nn}^2 (R_1 \parallel R_2)^2 + \frac{4kT}{R_1 \parallel R_2} (R_1 \parallel R_2)^2 \\ &= e_n^2 + i_{np}^2 R_3^2 + 4kT R_3 + i_{nn}^2 (R_1 \parallel R_2)^2 + 4kT (R_1 \parallel R_2) \\ &= e_n^2 + i_{np}^2 R_3^2 + i_{nn}^2 (R_1 \parallel R_2)^2 + 4kT (R_3 + R_1 \parallel R_2) \end{aligned}$$

For  $i_{np} = i_{nn} = i_n$ ,

$$e_{ni}^2 = e_n^2 + i_n^2 R_{s2}^2 + 4kTR_s$$

where  $R_s = R_3 + R_1 || R_2$ ,  $R_{s2}^2 = R_3^2 + (R_1 || R_2)^2$ .

- Setting  $R_3 = 0$  reduces noise.
- $e_n$  dominates for low values of  $R_s$ : it is called the *short-circuit noise*.
- For  $R_s \rightarrow \infty$ ,  $e_{ni} \approx i_n R_{s2}$ :  $i_n$  is called the *open-circuit noise*.

Noise is amplified by:

$$A_v = \frac{1 + \frac{R_2}{R_1}}{\sqrt{1 + (f/f_A)^2}} = \frac{A_0}{\sqrt{1 + (f/f_A)^2}}$$

The total output rms noise is

$$E_{no} = A_0 \times \sqrt{E_1^2 + E_2^2 + E_3^2 + E_4^2}$$

where

$$E_1^2 = e_{nw}^2 \left( f_{ce} \ln \frac{f_A}{f_L} + 1.57 f_A - f_L \right)$$

$$E_2^2 = R_3^2 i_{npw}^2 \left( f_{cip} \ln \frac{f_A}{f_L} + 1.57 f_A - f_L \right)$$

$$E_3^2 = (R_1 || R_2)^2 i_{nnw}^2 \left( f_{cin} \ln \frac{f_A}{f_L} + 1.57 f_A - f_L \right)$$

and

$$E_4^2 = 4kT(R_3 + R_1 || R_2)(1.57 f_A - f_L)$$

Book says:  $f_L$  is  $1/T_{obs}$  where  $T_{obs}$  is the averaging time used to measure the output.

TI Application note says: take  $f_H/f_L = NEB$ .

For low-noise designs, use op amps with low  $e_{nw}$  and low corner frequencies  $f_{ci}$  and  $f_{cn}$ .

The *total rms input noise* can be obtained by dividing by the signal dc gain  $A_{s0}$

$$E_{ni} = \frac{E_{no}}{|A_{s0}|}$$

and the signal-to-noise ratio from

$$SNR = 20 \log_{10} \frac{V_{i(rms)}}{E_{ni}}$$