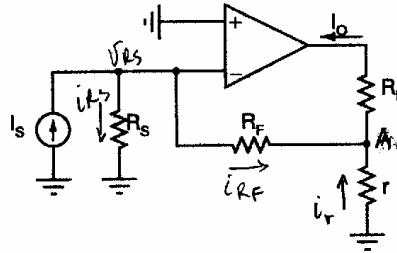


Electrical and Computer Engineering Department  
 University of Puerto Rico - Mayaguez, P.R.  
 Electronics II - INEL 4202 - SPRING 2002 - Final Exam - Prof. Manuel Toledo  
**THIS EXAM CONTAINS FOUR PROBLEMS FOR A TOTAL OF 105 POINTS**  
**WORK CLEARLY OR LOOSE POINTS**

1. The following circuit shows how to design a current amplifier using an op-amp and current-sampling, current-mixing (*shunt-series*) feedback.



- (a) Show, without using feedback theory but assuming an ideal op-amp, that the current gain is given by (15 points)

$$\frac{I_O}{I_S} = 1 + \frac{R_F}{r}$$

- (b) Show that feedback theory predicts the gain to be the expression given in part (a) when the op-amp gain is taken to be very large. (HINT: the feedback network is composed of resistors  $r$  and  $R_F$ .) (5 points)
- (c) Using The feedback-analysis method find the closed-loop gain  $\frac{I_O}{I_S}$ , the input resistance (excluding  $R_S$ ), and the output resistance (excluding  $R_L$ ) for the case: open-loop gain of op-amp =  $10^4 V/V$ , differential input resistance for op-amp  $R_{id} = 100k\Omega$ , op-amp output resistance =  $1k\Omega$ ,  $R_S = R_L = 10k\Omega$ ,  $r = 100\Omega$ , and  $R_F = 1k\Omega$ . (20 points)

Answer

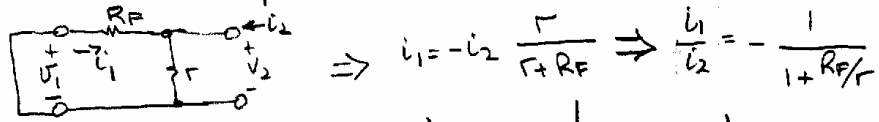
(a) Since  $V_- = V_+ = 0V$ ,  $V_{R_S} = 0$  and  $i_{R_S} = 0$ ,  $\therefore i_{R_F} = I_S$ .

and  $V_A = -I_S R_F$ . KCL at node A yields  $I_O = i_r + i_{R_F}$ ,

or

$$I_O = I_S + \frac{-V_A}{r} = I_S + I_S \frac{R_F}{r} \Rightarrow \boxed{\frac{I_O}{I_S} = 1 + \frac{R_F}{r}}$$

(b) For  $A\beta \gg 1$ ,  $A_f \approx 1/\beta$ . For shunt-series feedback,  $\beta = \frac{i_1}{i_2} \Big|_{v_1=0}$



$$\Rightarrow i_1 = -i_2 \frac{r}{r + R_F} \Rightarrow \frac{i_1}{i_2} = -\frac{1}{1 + R_F/r}$$

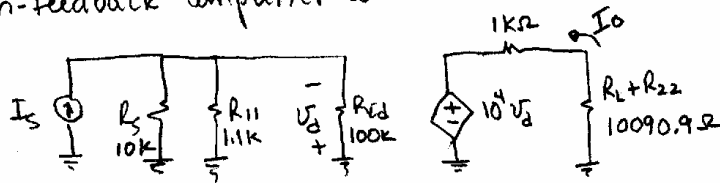
Observing that  $I_o = -i_2 \Rightarrow \beta = \frac{1}{1 + R_F/r}$  and

$$A_f \approx \frac{1}{\beta} = 1 + R_F/r$$

(c)  $R_{11} = \frac{v_1}{i_1} \Big|_{i_2=0} = R_F + r = 1.1 \text{ k}\Omega$  ;  $R_{22} = \frac{v_2}{i_2} \Big|_{v_1=0} = R_F \parallel r = 90.9 \Omega$

$$\beta = \frac{1}{1 + R_F/r} = \frac{1}{1 + 1 \text{ k}\Omega / 100 \Omega} = \frac{1}{11}$$

The non-feedback amplifier is



$$I_o = -10^4 v_d / 11090.9 \Omega ; v_d = -100 \text{ k} (I_s) \frac{10 \text{ k} \parallel 1.1 \text{ k}}{100 \text{ k} + 10 \text{ k} \parallel 1.1 \text{ k}} = -981.3 I_s$$

$$\therefore A_I = \frac{I_o}{I_s} = \left( \frac{-10^4}{11090.9 \Omega} \right) (-981.3 \Omega) = +884.75 \text{ A/A}$$

$$D = 1 + \beta A = 1 + \frac{1}{11} \times 884.75 = 81.43$$

$$A_f = \frac{I_o}{I_s} = \frac{A}{D} = \frac{884.75}{81.43} = 10.87 \text{ A/A}$$

$$R_{if} = \frac{R_i}{D} = \frac{10 \text{ k} \parallel 1.1 \text{ k} \parallel 100 \text{ k}}{81.43} = 12 \Omega \Rightarrow R_{in} = \left( \frac{1}{R_{if}} - \frac{1}{R_s} \right)^{-1} = \left( \frac{1}{12} - \frac{1}{10 \text{ k}} \right)^{-1} \approx 12 \Omega$$

$$R_{of} = R_o \times D = 11090.9 \Omega \times 81.43 = 903 \text{ k}\Omega ;$$

$$R_{out} = R_{of} - R_L = 903 \text{ k}\Omega - 10 \text{ k}\Omega = 893 \text{ k}\Omega$$

2. Consider a feedback amplifier for which the open-loop gain  $A(s)$  is given by

$$A(s) = \frac{1000}{(1 + s/10^4)(1 + s/10^5)^2}$$

If the feedback factor  $\beta$  is independent of frequency, find

- (a) the frequency at which the phase shift is  $180^\circ$ , (10 points) and  
 (b) the critical value of  $\beta$  at which instability will begin. (10 points)

$$(a) \phi = \tan^{-1}\left(\frac{\omega}{10^4}\right) + 2 \tan^{-1}\left(\frac{\omega}{10^5}\right) = 180^\circ$$

We need to find  $\omega$ . If we express this eq. as

$$\omega = 10^5 \tan\left(90^\circ - \frac{1}{2} \tan^{-1}\left(\frac{\omega}{10^4}\right)\right)$$

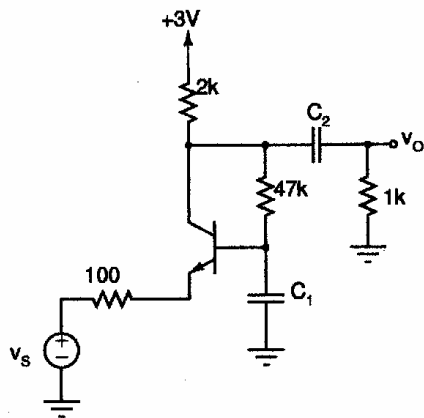
we can try to solve recursively. The solution converges to  $\omega = 109544.5 \text{ rps}$ . The phase angle at this freq. is indeed  $180^\circ$ , as can be verified by direct substitution.

(b) At  $\omega = 109544.5 \text{ rps}$

$$|A| = \frac{1000}{\sqrt{1 + \left(\frac{109544.5}{10^4}\right)^2} \left(\sqrt{1 + 1.095445^2}\right)^2} = 41.32$$

$\therefore$  The critical value of  $\beta$  is  $\frac{1}{41.32}$ , or  $0.0242$

3. For the common-base circuit shown below, assuming that the bias collector current to be about 1 mA,  $\beta = 100$ ,  $C_{\mu} = 0.8 \text{ pF}$ ,  $f_T = 600 \text{ MHz}$ ,  $C_1 = 1 \mu\text{F}$  and  $C_2 = 10 \mu\text{F}$ :



- (a) Determine the midband gain  $v_o/v_s$ . (5 points)  
 (b) Use the short-circuit time-constant method to estimate the lower 3-dB frequency,  $f_L$ . (15 points)  
 (c) Find the high-frequency poles, and estimate the upper 3-dB frequency,  $f_H$ . (15 points)

(a) Since the circuit is a common-base amplifier,  $A_v = \frac{v_o}{v_s} = +g_m R_c$   
 The overall mid-band gain is

$$\frac{v_o}{v_s} = \left(\frac{1}{25}\right) (2\text{k} \parallel 1\text{k} \parallel 47\text{k}) \left(\frac{25}{125}\right) = \boxed{+5.26 \text{ V/V}}$$

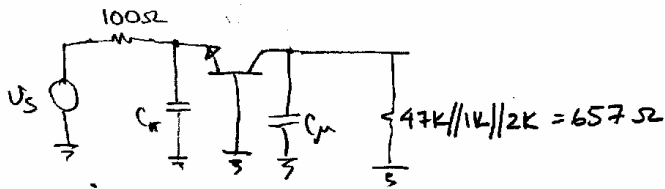
(b)  $C_1$  sees  $[r_{\pi} + (\beta + 1)100] \parallel [47\text{k} + 2\text{k} \parallel 1\text{k}] = 12.6\text{k} \parallel 47.7\text{k} \approx 9966 \Omega$

$$\therefore \omega_{L1} = \frac{1}{9966 \Omega \times 10^{-6} \text{ F}} = \boxed{100.3 \text{ rps}}$$

$C_2$  sees  $1\text{k} + 2\text{k} \parallel 47\text{k} \Rightarrow \omega_{L2} = \frac{1}{10 \mu\text{F} \times 2.92\text{k}} = \boxed{34.3 \text{ rps}}$

$$\therefore \omega_L \approx \omega_{L1} + \omega_{L2} = \boxed{134.6 \text{ rps}}$$

(c) At high. freqs, the circuit looks as follows



$$C_\pi \text{ sees } \frac{1}{g_m} \parallel 100\Omega = 25\Omega \parallel 100\Omega = 20\Omega$$

$$C_\mu \text{ sees } 657\Omega$$

$$\text{To find } C_\pi, \text{ observe that } f_T = \frac{P_0}{2\pi C_\pi (C_\mu + C_\pi)} = \frac{100}{(5k)\pi (.8pF + C_\pi)}$$

$$C_\pi = \frac{100}{5000\pi (600)(10^6)} - .8pF = 9.8pF$$

So that

$$\omega_\pi = \frac{1}{9.8pF \times 20\Omega} = 5.1 \times 10^9 \text{ rps}$$

and

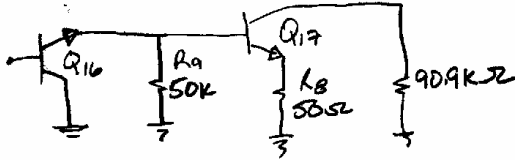
$$\omega_\mu = \frac{1}{.8pF \times 657\Omega} = 1.9 \times 10^9 \text{ rps}$$

Since they are less than 2 octaves away,

$$\omega_\pi = \frac{1}{\frac{1}{\omega_\pi} + \frac{1}{\omega_\mu}} = \boxed{1.3 \times 10^9 \text{ rps}} = \boxed{220 \text{ MHz}}$$

4. Consider a variation on the design of the 741 second stage in which  $R_8 = 50\Omega$ . What will be the corresponding input resistance  $R_{i2}$  and trans-resistance  $R_{m2}$  of the second stage? (10 points)

From class, we know that  $I_{B3} \approx 550\mu A \Rightarrow r_{o13B} = \frac{50V}{550\mu A} = 90.9k\Omega$   
is the load of  $Q_{17}$ . The second stage is as follows, for a.c.



$$g_{m17} = \frac{550\mu A}{25mV} = \frac{.55 A}{25 V}$$

To find the gain, we must first estimate the collector current of  $Q_{16}$ . From  $V_{E17} \approx 50\Omega (550\mu A) = 0.0275V = 27.5mV$  and

$$V_{BE17} = V_T \ln\left(\frac{I_{C17}}{I_S}\right) = 25mV \ln\left(\frac{550\mu A}{10^{-14} A}\right) = 618mV, \text{ we get that}$$

$$V_{E16} = 618mV + 27.5mV = 645.8mV. \text{ Thus } I_{R9} = \frac{.6458V}{50k\Omega} = 12.9\mu A.$$

$$\text{Since } I_{B17} = \frac{550\mu A}{\beta_N} = \frac{550\mu A}{200} = 2.75\mu A, I_{E16} = 15.65\mu A \text{ and}$$

$$g_{m16} = 6.26 \times 10^{-4} A/V.$$

The input resistance is

$$R_{in2} = r_{\pi 16} + (\beta_N + 1) \left[ 50k\Omega \parallel (r_{\pi 17} + (\beta_N + 1) 50\Omega) \right] =$$

$$= 1319.8k\Omega + (201) \left[ 50k\Omega \parallel (9k\Omega + 201 \times 50) \right] = \boxed{3.1M\Omega}$$

$$R_{m2} = R_{in2} A_{v2} = 3.1M\Omega \left( \frac{g_{m16} [50k\Omega \parallel (9k\Omega + 201 \times 50)]}{1 + g_{m16} [50k\Omega \parallel (9k\Omega + 201 \times 50)]} \right) \left( \frac{-g_{m17} (90.9k\Omega)}{1 + g_{m17} (50\Omega)} \right)$$

$$= -3.1 \times 10^6 \times 0.897 \times 952 = \boxed{-2.66\Omega}$$