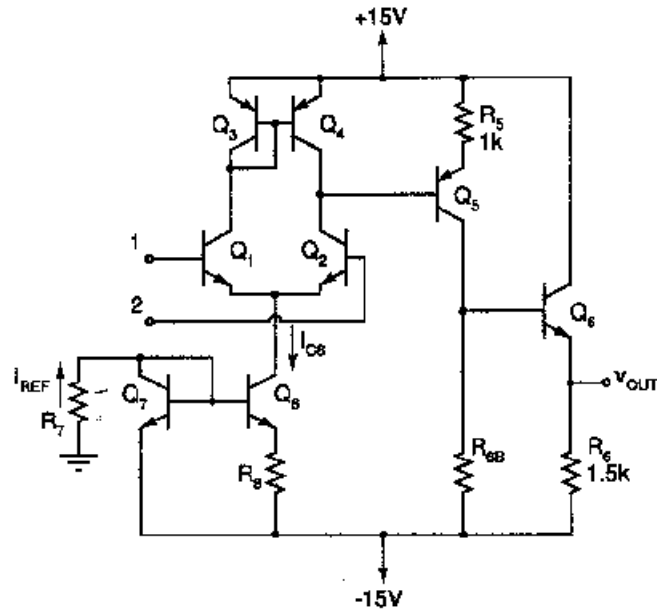


Electrical and Computer Engineering Department
 University of Puerto Rico - Mayaguez, P.R.
 Electronics II - INEL 4202 - SPRING 2002 - Exam 3A - Prof. Manuel Toledo
THIS EXAM CONTAINS 15 BONUS POINTS - WORK CLEARLY OR LOOSE POINTS

The transistors in the amplifier shown below have $\beta = 100$. Base currents can be neglected in your analysis. Assume that Q_5 is biased such that $I_{C5} = \frac{\beta}{\beta+2} I_{C8}$.



1. Assuming $R_7 = 72k\Omega$, $R_{EB} = 10k\Omega$, $R_E = 0$, $V_A = 100V$ and that the area of Q_6 equals 5 times the area of Q_7 , find:
 - (a) the differential gain $A_d = \frac{v_{OUT}}{v_1 - v_2}$ (50 points)
 - (b) the input resistance R_{in} seen by differential signals between terminals 1 and 2. (25 points)
 - (c) the output resistance R_{out} at the output terminal, neglecting the resistance seen into the collector of Q_5 . (25 points)
 - (d) v_{OUT} when $v_1 = v_2 = 0$. (15 points)

lavé 3A

① First find the op. point currents

$$I_{REF} = \frac{14.3}{72k\Omega} \approx 0.2 \text{ mA} \Rightarrow I_{C8} = 5 \times 0.2 \text{ mA} = 1 \text{ mA}$$

$$I_{C2} = 0.5 \text{ mA} \Rightarrow g_{m2} = \frac{0.5 \text{ mA}}{25 \text{ mV}} = \frac{1}{50} \text{ A/V}$$

$$I_{C5} = \frac{100}{102} \times 1 \text{ mA} = 0.98 \text{ mA} \Rightarrow g_{m5} = 0.0392 \text{ A/V}$$

$$V_{C5} = 10k \times I_{C5} - 15 = -5.2 \text{ V}$$

$$I_{C6} = \frac{-5.2 - 1.76 - (-15)}{1.5k\Omega} = 6.07 \text{ mA}$$

$$g_{m6} = 0.243 \text{ A/V}$$

$$r_{o2} = r_{o4} \approx \frac{V_A}{I_{C2}} = \frac{100 \text{ V}}{0.5 \text{ mA}} = 200k\Omega$$

$$R_{in \text{ bases}} = r_{\pi 5} + 101k = \frac{100}{0.0392} + 101k = 103.55k\Omega$$

$$\begin{aligned} \frac{V_{C2}}{V_1 - V_2} &= g_{m2} (r_{o2} \parallel r_{o4} \parallel R_{in \text{ bases}}) \\ &= \left(\frac{1}{50} \text{ A/V}\right) (100k \parallel 103.55k) = +1017.4 \text{ V/V} \end{aligned}$$

$$\frac{V_{C5}}{V_{C2}} = \frac{-g_{m5} R_{C5}}{1 + g_{m5} R_{C5}}$$

$$\begin{aligned} R_{C5} &= 10k\Omega \parallel \left(\frac{100}{0.243} + 101 \times 1.5k\right) \approx 152k\Omega \parallel 10k \\ &= 9382\Omega \end{aligned}$$

$$\frac{V_{C5}}{V_{C2}} = \frac{-0.0392 \times 9382}{1 + 0.0392 \times 1000} = -9.15 \text{ V/V}$$

$$\frac{V_{ec}}{V_{cs}} = \frac{+g_{m6} R_6}{1 + g_{m6} R_6} = \frac{.243 \times 1500}{1 + .243 \times 1500} = 0.997$$

$$A_d = .10174 \times (-9.15)(0.997) = \boxed{-9283.7 \text{ V/V}}$$

$$(b) R_{in} = 2r_{\pi 2} = 2 \frac{100}{1/50} \Omega = \boxed{10 \text{ K}\Omega}$$

$$(c) R_{out} = 1.5 \text{ K}\Omega \parallel \frac{r_{\pi 6} + R_{6B}}{101} = 1.5 \text{ K}\Omega \parallel \left(\frac{\frac{100}{.243} + 10 \text{ K}}{101} \right)$$

$$= \boxed{96.5 \Omega}$$

$$(d) V_{out} = V_{cs} - .7 = -5.2 \text{ V} - 0.7 \text{ V} = \boxed{-5.9 \text{ V}}$$