



A MIMO Modeling Framework Using a Software Defined Radio Paradigm

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Outline

- Motivation
- Objectives
- Background
- Methodology
- Design
- Implementation
- Testing
- Conclusions

Motivation



Motivation

- Multiple Input Multiple Output (MIMO): use of multiple antennas, both, at transmitter and receiver.
 - MIMO is a trending technology into the signal communications realm.
 - Actual implementations with 3GPP, WiMAX, WiFi.
- Software Defined Radio
 - Radio implemented by means of software.
- Time-frequency Representations

Objectives

- Design, implement, and test a framework for MIMO channel monitoring and simulation
 - Redesign the existent **S**ignal **R**epresentation **L**ABoratory application software named **SIRLAB**.
 - Implement time-frequency Representations.
 - Provide a MIMO simulation.

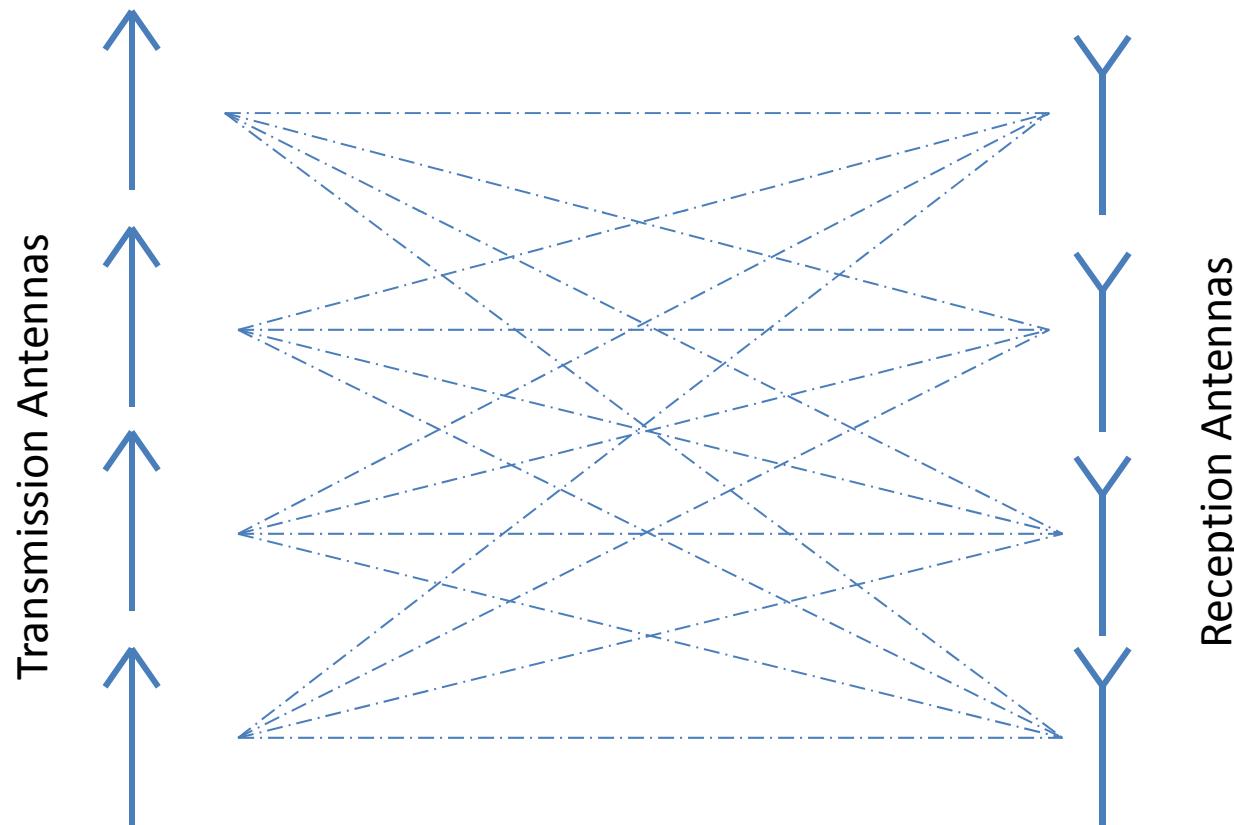
Background

- Communications
- Software Defined Radio
- Time-Frequency Representations

Communications

- Communications
 - Send multiple symbols with different antennas.
 - The signal is modified by the channel and possibly reflected by several scatterers.
 - Multiple copies of the signal may be received and processed.

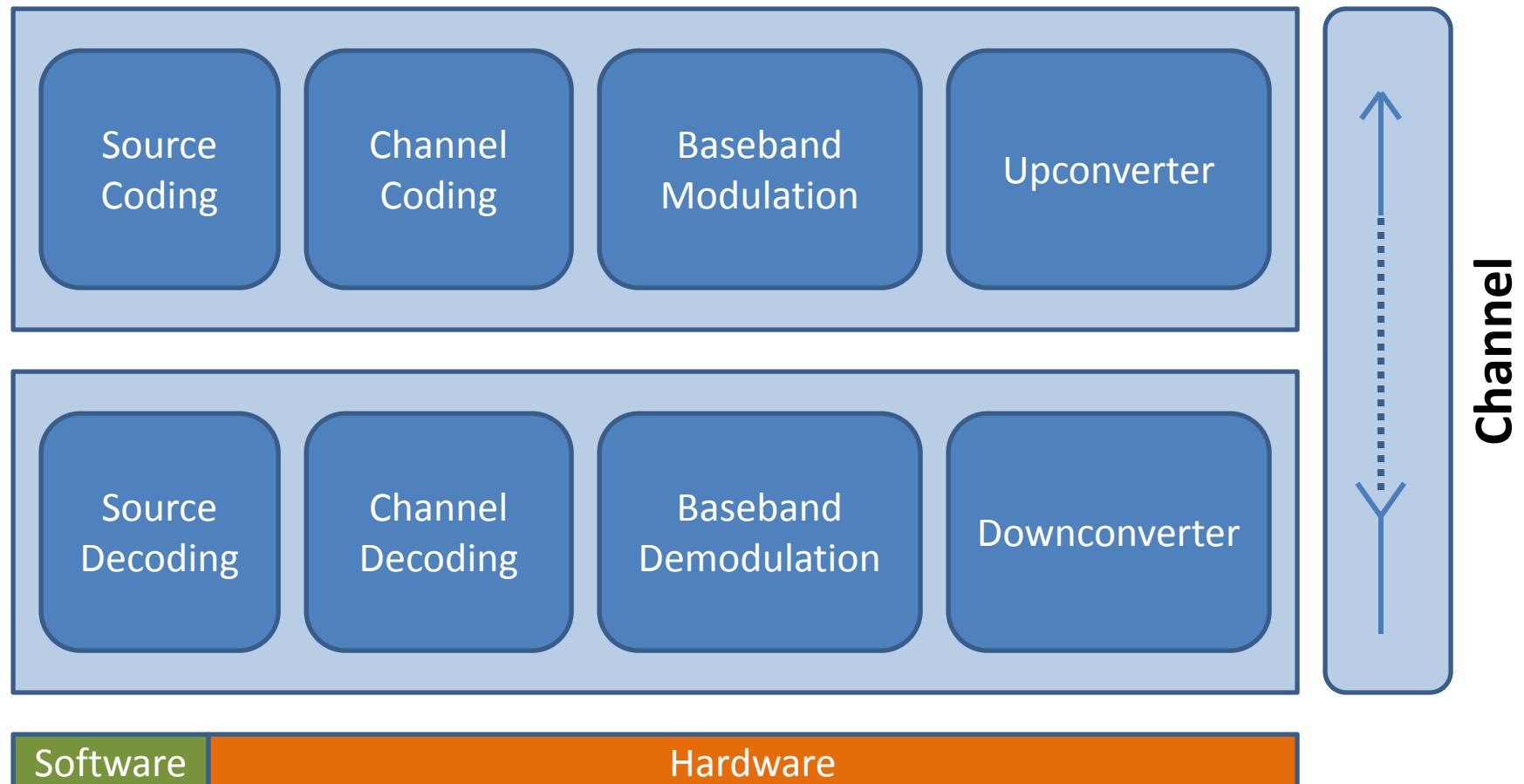
Communications Channel



Software Defined Radio

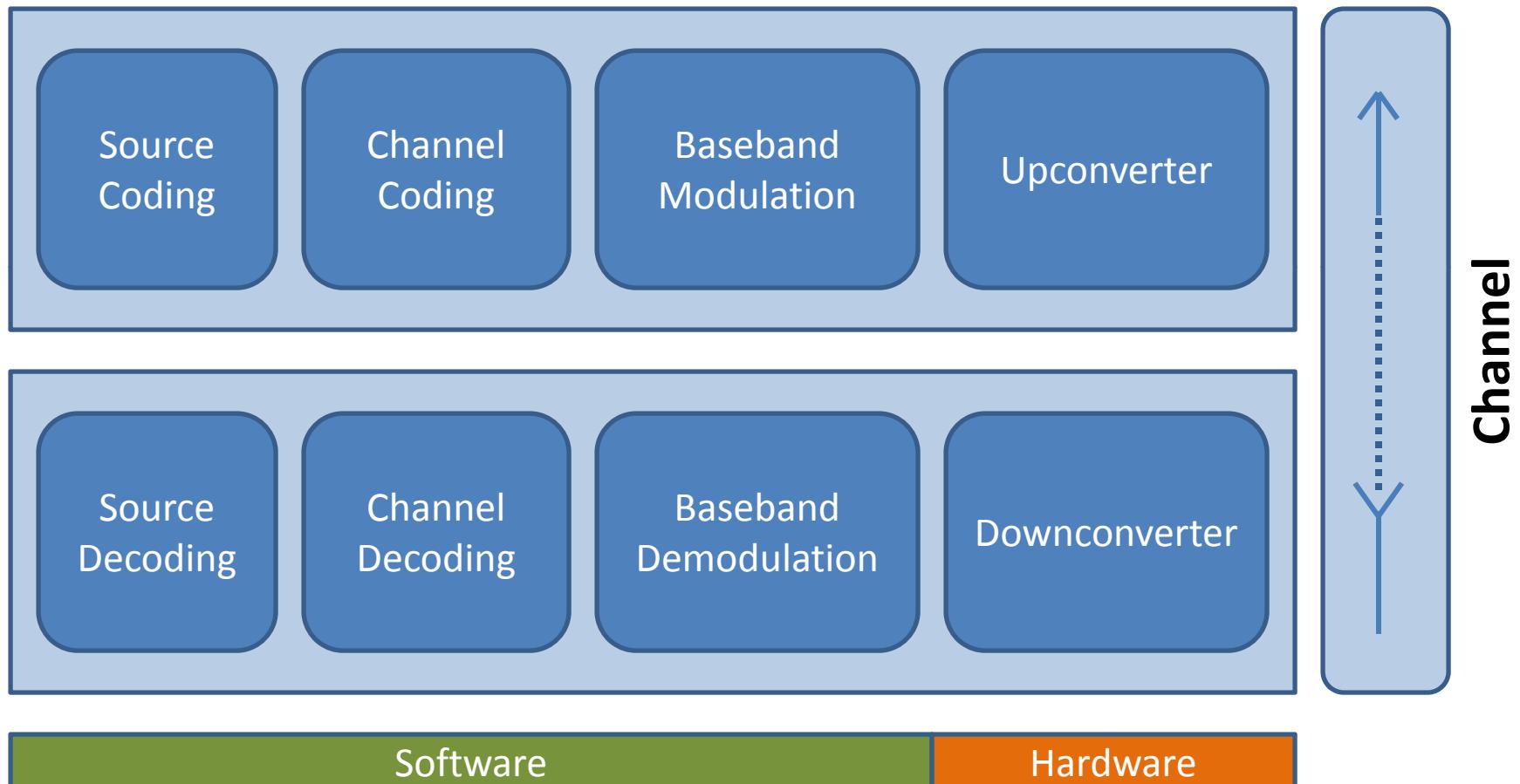
- Like traditional radio
 - It does what a typical radio does.
- Unlike traditional radio
 - Several components have been implemented computationally.
- Software can perform jobs that before were done by hardware.
- Extending the software towards the antenna

Traditional Radio



Traditional Radio Paradigm

Software Defined Radio



SDR Paradigm

Software Defined Radio Tools

- SoRa, by Microsoft
- Simulink, by MATLAB
- GNURadio, as an Open Source

Software Defined Radio Implementation

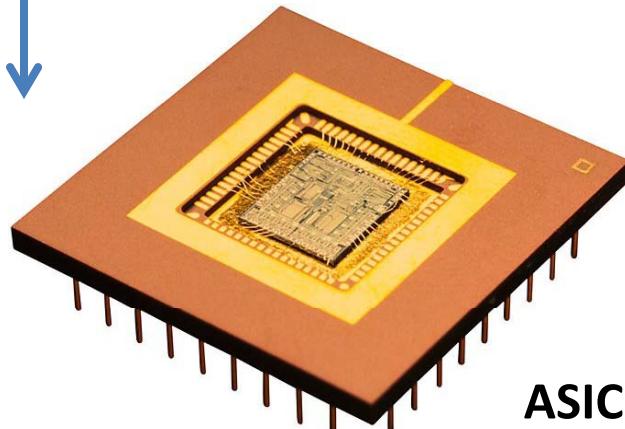
```
#include "civclient.h"

/* this is used in strange places,
   needed (hence, it is not 'extern')
bool is_server = FALSE;

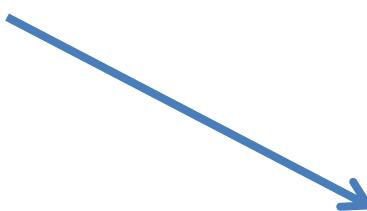
char *logfile = NULL;
char *scriptfile = NULL;
static char tileset_name[512] = "\0";
char sound_plugin_name[512] = "\0";
char sound_set_name[512] = "\0";
char server_host[512] = "\0";
char user_name[512] = "\0";
char password[MAX_LEN_PASSWORD] = "\0";
char metaserver[512] = "\0";
int server_port = -1;
bool auto_connect = FALSE; /* TRUE = skip "C
bool in_ggz = FALSE;
```



FPGA



ASIC



Personal Computer

Software Defined Radio Implementation



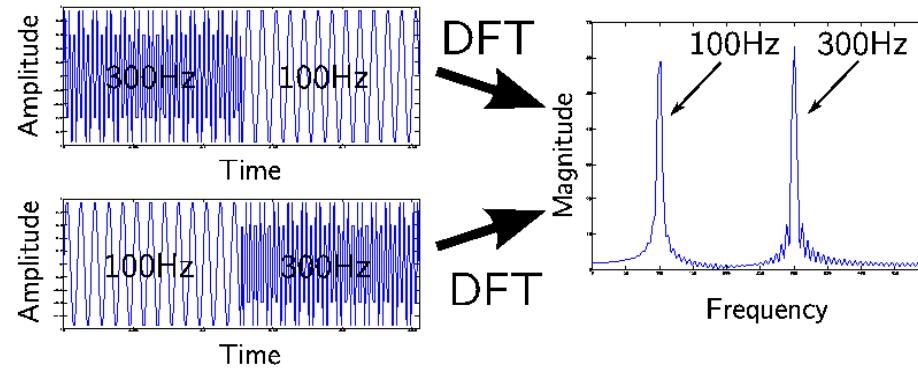
Personal Computer

Time-Frequency Representations

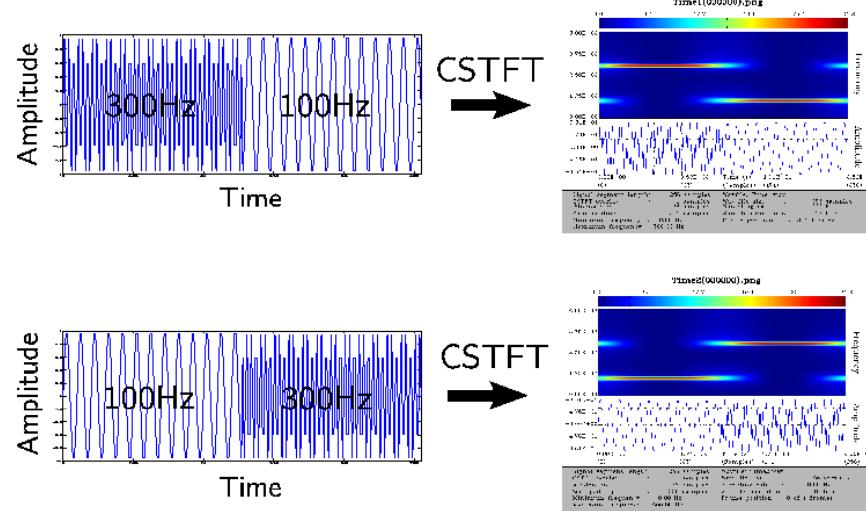
- Techniques and methods
- Signals whose characteristics are changing with time
- Allow to extract additional information
- High computational requirements

Time-Frequency Representations

**NO
DISCRIMINATION**



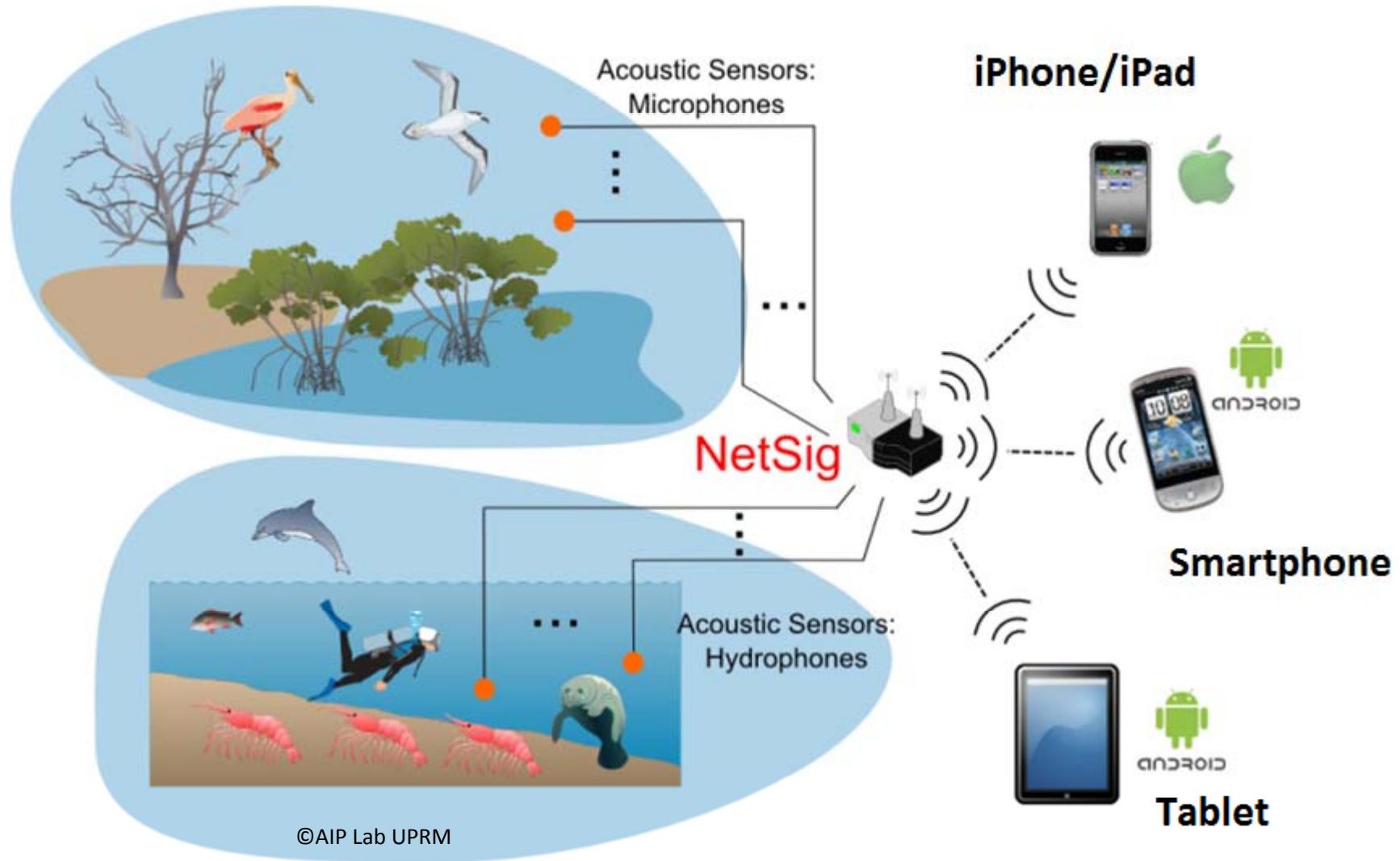
DISCRIMINATION



Methodology

- Available tools
 - SIRLAB, by the AIP Lab
 - GNURadio, as an Open Source
- Preliminary Results
 - SIRLAB Parallelization
 - User Integration: webSIRLAB, SIRDroid
- Framework for MIMO channel monitoring and simulation
 - Design
 - Implementation
 - Testing

SIRLAB on a NetSig Node Processor



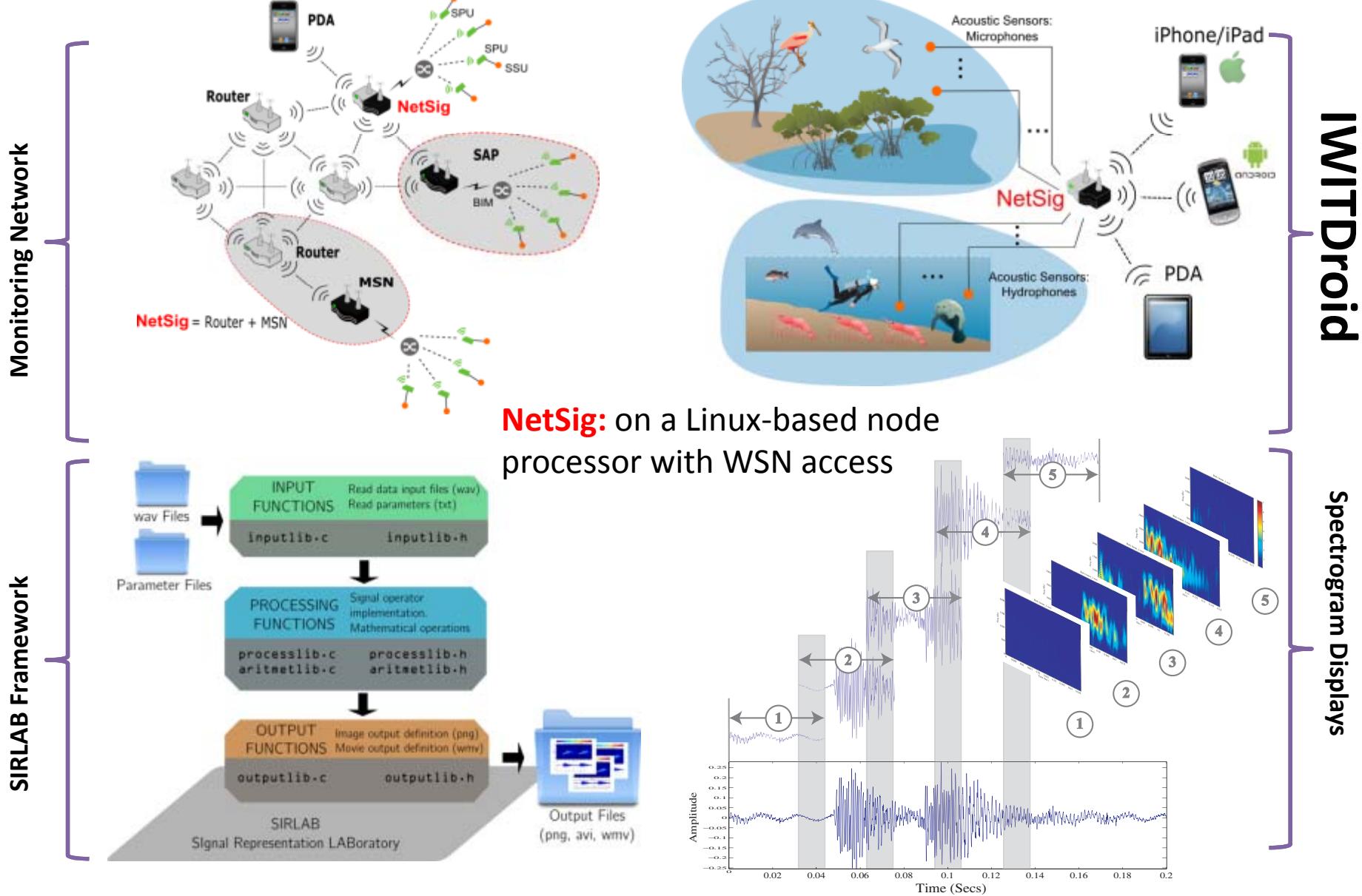
SIRLAB

SIRLAB: A Tool for Research and Education

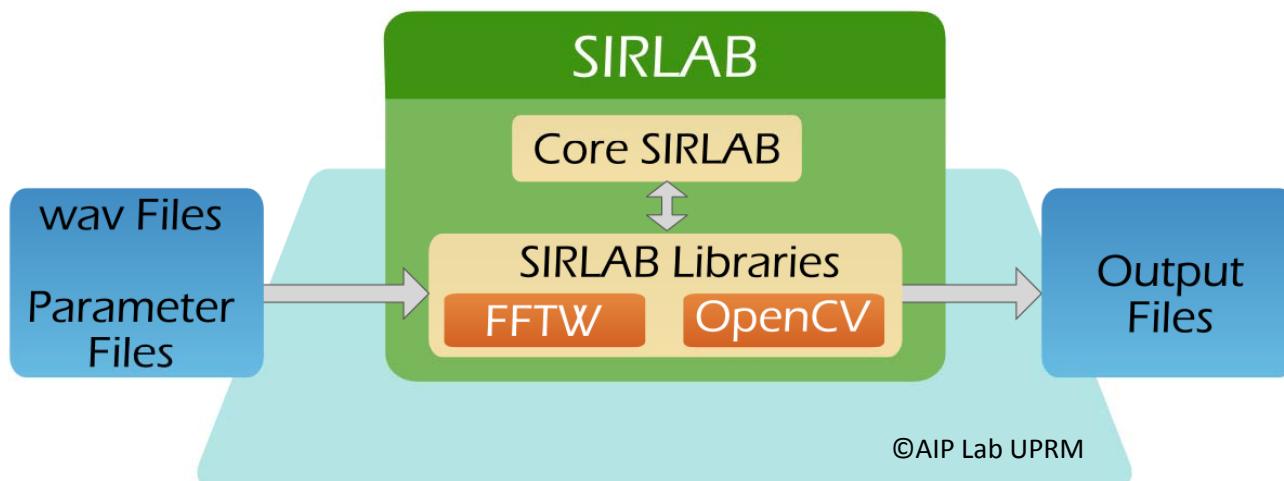
- **SIRLAB:** SIgnal Representation LABoratory
- Open-Source Framework Developed at the AIP Lab
- Research Tool for Time-Frequency Analysis
- Educational Tool for Signal Representation
- Based on OpenCV and FFTW Software Libraries
- Uses R. Tolimieri's Theory on Time-Freq. Repres.
- **Input Format:** WAV File
- **Language Written:** C/C++
- **Speed Up Time:** 20+ Times Faster than Most Known MATLAB-based Time-Frequency Tools

- Known Time-Frequency (T-F) Toolboxes
 - <http://tftb.nongnu.org> (TFTB)
 - Developed by *Rice Univ.*: <http://dsp.rice.edu/> & *CN Recherche Scientifique*: <http://www.cnrs.fr/>
 - <http://espace.library.uq.edu.au/view/UQ:211321>
 - T-F Signal Analysis (TFSA) Matlab Toolbox v.5.5
 - Developed by *Univ. of Queensland*: uq.edu.au/
 - <http://www.mathworks.com/matlabcentral>
 - DiscreteTFDs – T-F Signal Analysis Software
 - Developed by *Jeff O'Neill*: jco8@cornell.edu

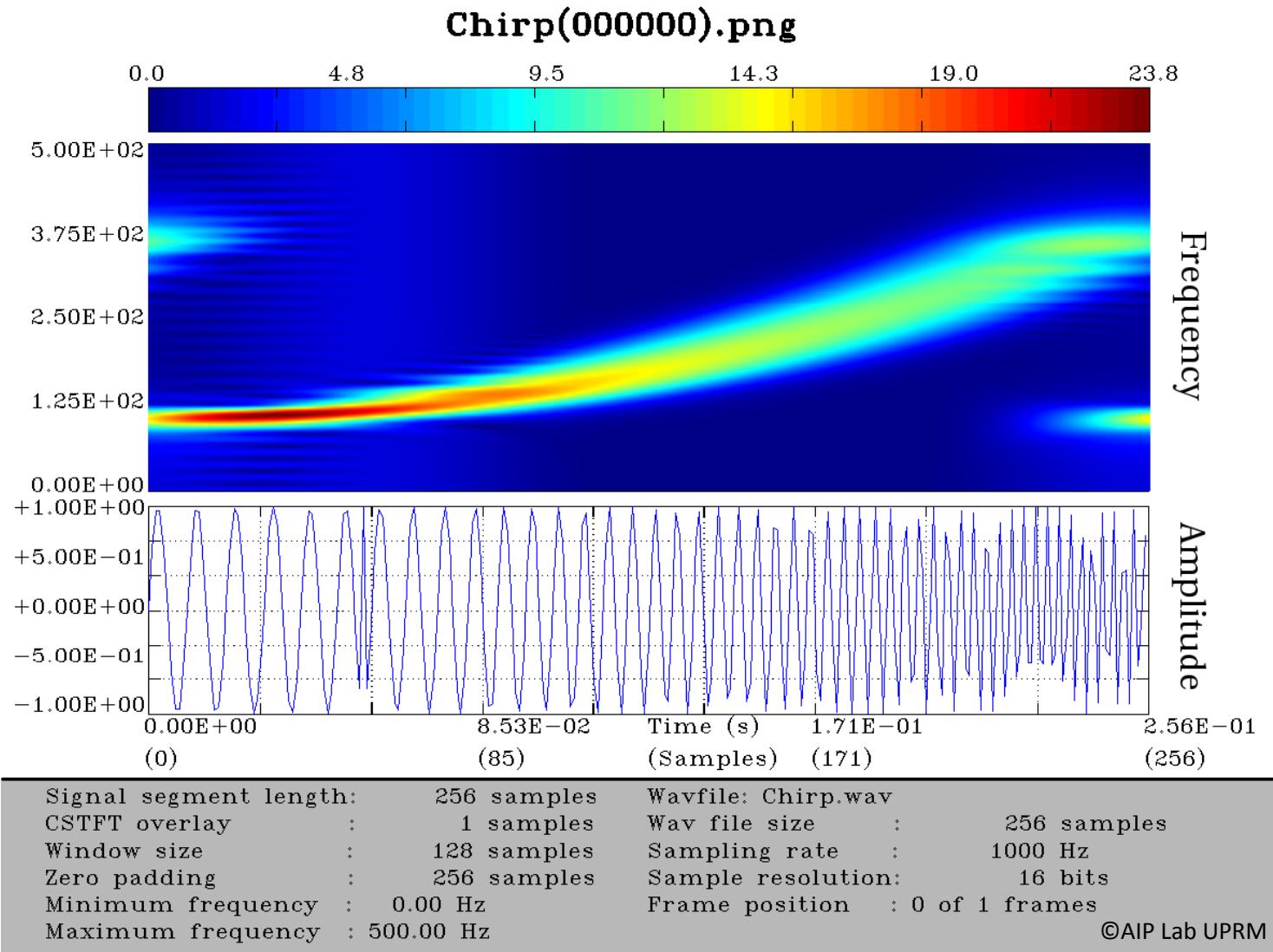
SIRLAB: Running on a NetSig Node



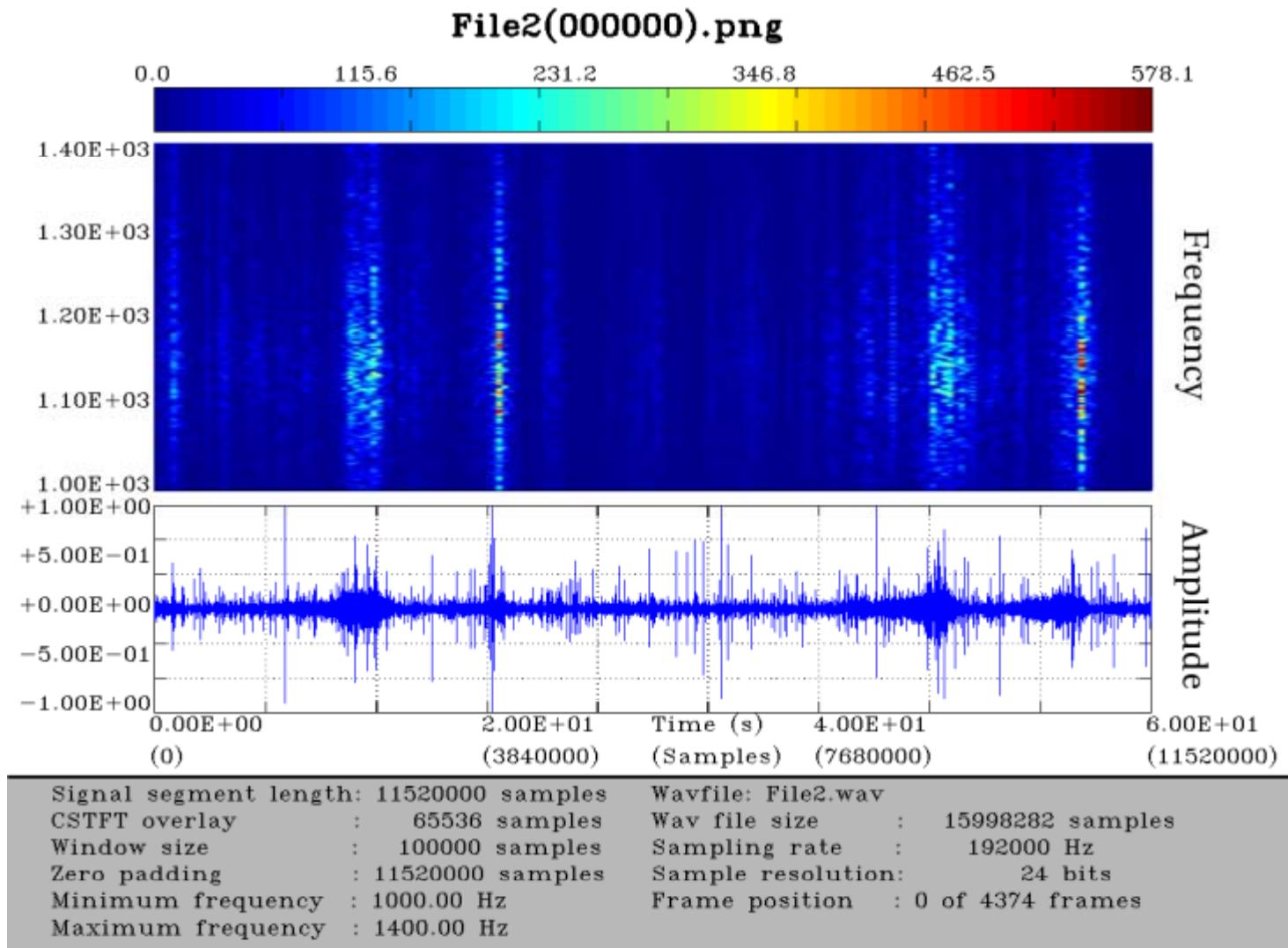
SIRLAB Architecture



SIRLAB Frame Example

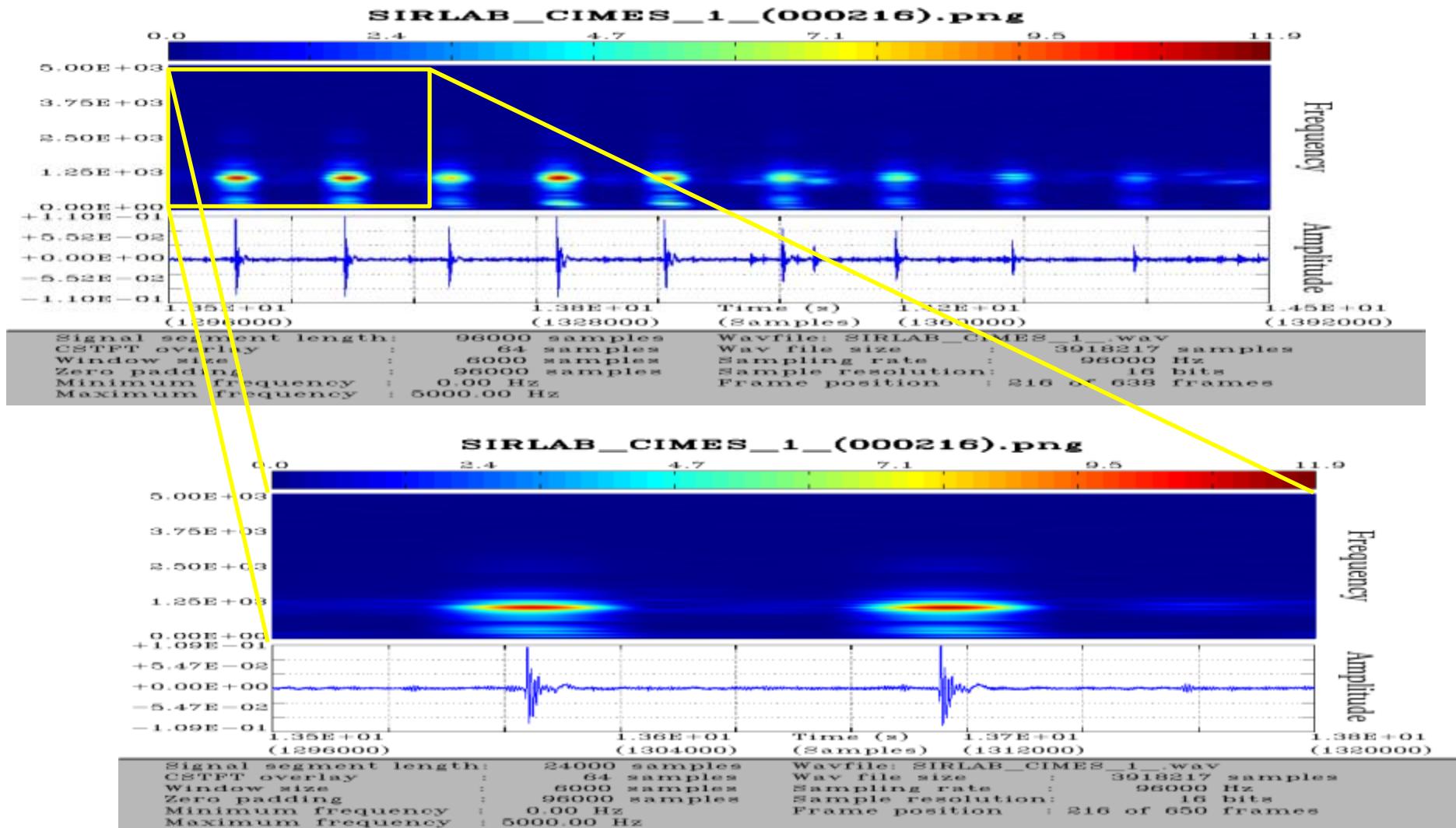


SIRLAB's Standard Output

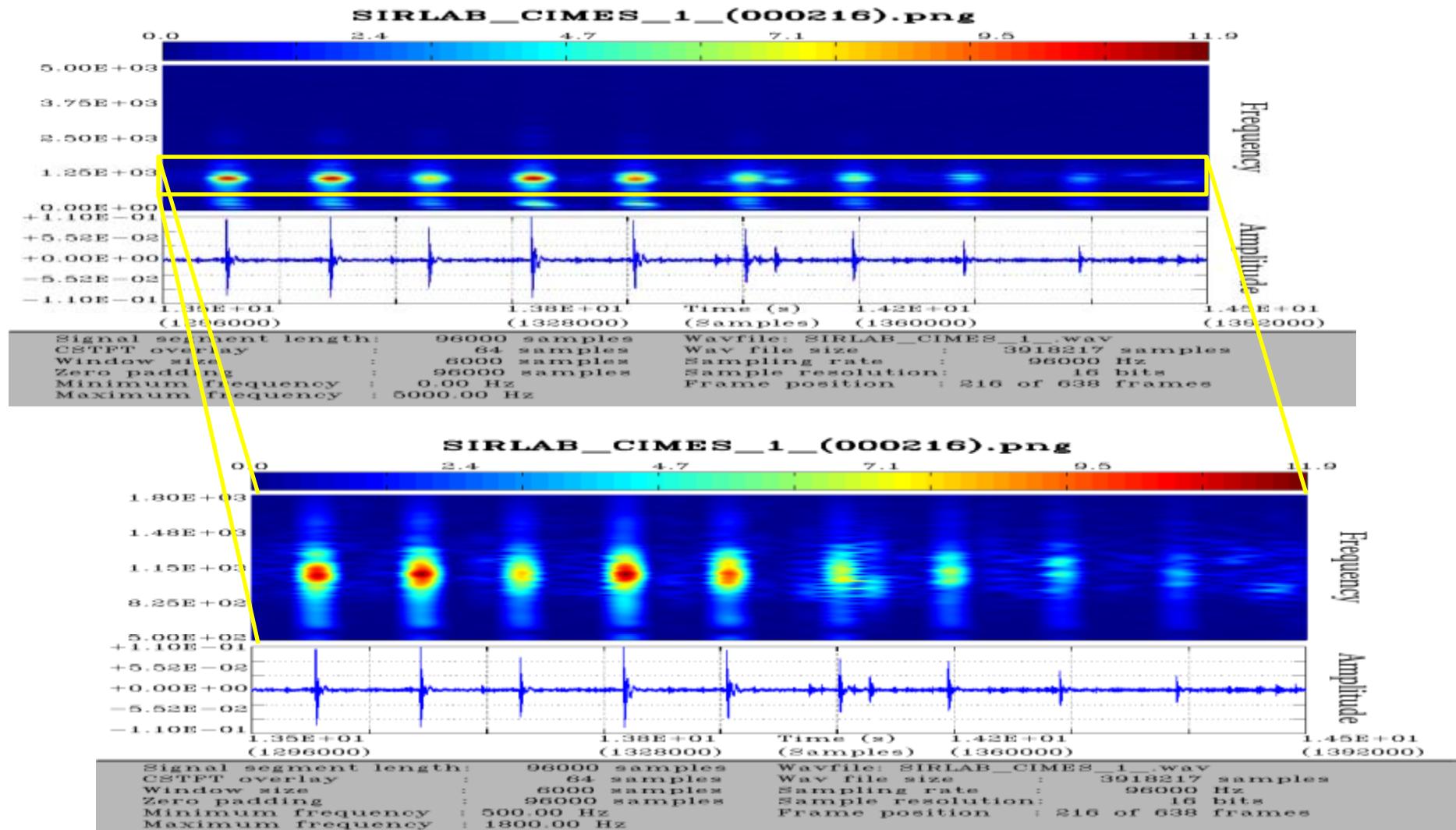


Sea waves...

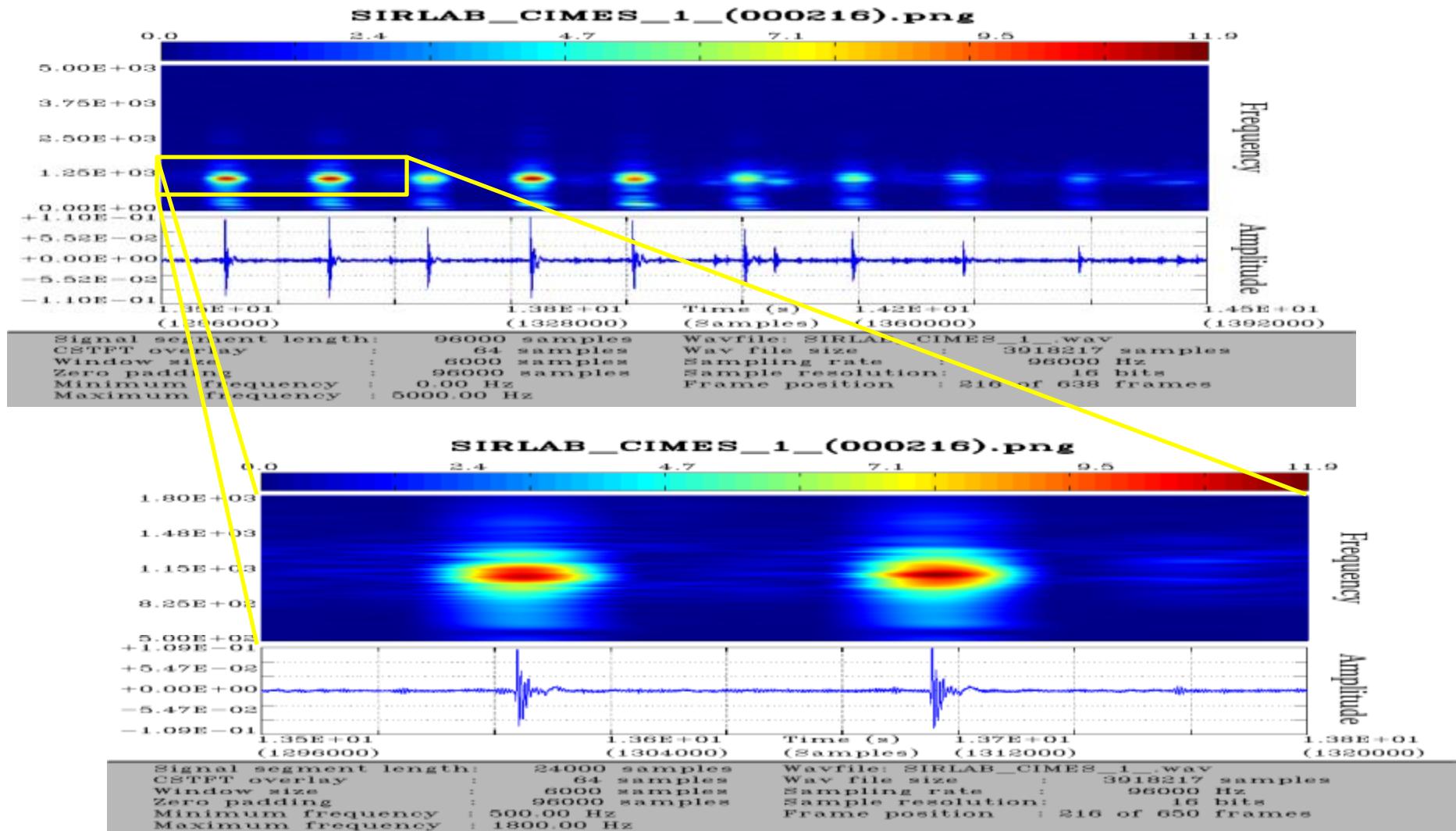
Frame Magnification: Time



Frame Magnification: Frequency



Frame Magnification: Time & Frequency



SIRLAB Challenges

- Parallelization Into Multiple Cores
- Improve the User Experience
 - Minimum Installation Effort
 - User Friendly Interaction
- Client – Server Architecture
- Integration with Mobile Devices

webSIRLAB

- Web Interface for SIRLAB
- Client Server Architecture
- Flexible Parameter Selection
- Easy Signal Submission for Processing at Server
- Friendly Display for Results
- Minimum Installation Effort
 - Modern **html5** web browser is required.

Research contribution

webSIRLAB's User Interface

The screenshot shows the webSIRLAB user interface. On the left, there is a form with various input fields and a preview area. On the right, there is a grid of spectrograms and a control bar.

SIRLAB

Num Samples frame:

Jump Samples:

Window Width:

Zero Padding:

Min Freq:

Max Freq:

Frame Overlay:

Start Percent:

Start Percent:

Wav File:

localhost/sirlab.php

Star icon

Wrench icon

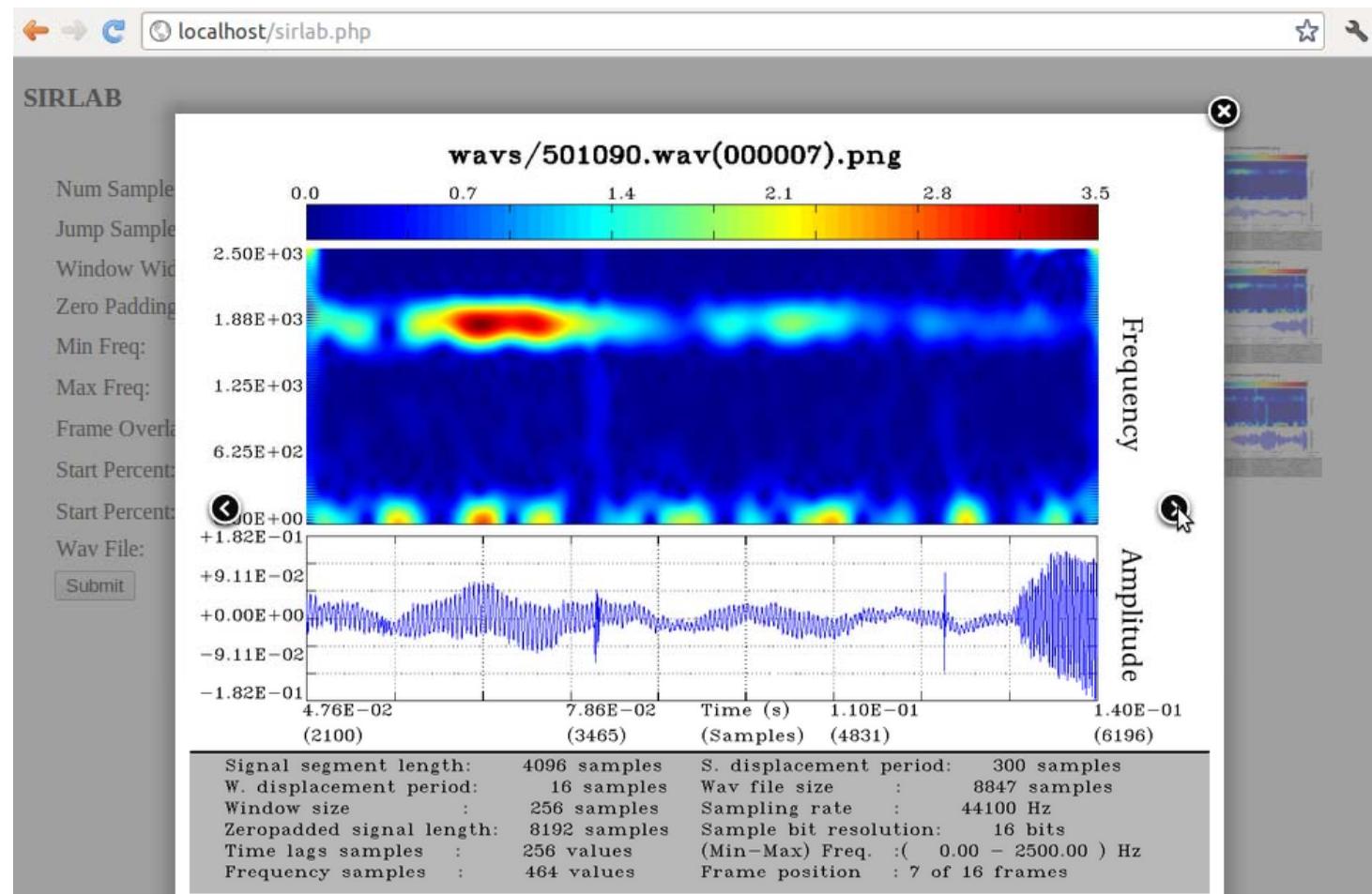
Three rows of five spectrograms each, labeled as follows:

- Row 1: Ecuad_Tropical_Acoustic001.png, Ecuad_Tropical_Acoustic002.png, Ecuad_Tropical_Acoustic003.png, Ecuad_Tropical_Acoustic004.png, Ecuad_Tropical_Acoustic005.png
- Row 2: Ecuad_Tropical_Acoustic006.png, Ecuad_Tropical_Acoustic007.png, Ecuad_Tropical_Acoustic008.png, Ecuad_Tropical_Acoustic009.png, Ecuad_Tropical_Acoustic010.png
- Row 3: Ecuad_Tropical_Acoustic011.png, Ecuad_Tropical_Acoustic012.png, Ecuad_Tropical_Acoustic013.png, Ecuad_Tropical_Acoustic014.png, Ecuad_Tropical_Acoustic015.png

Control bar: 00:00

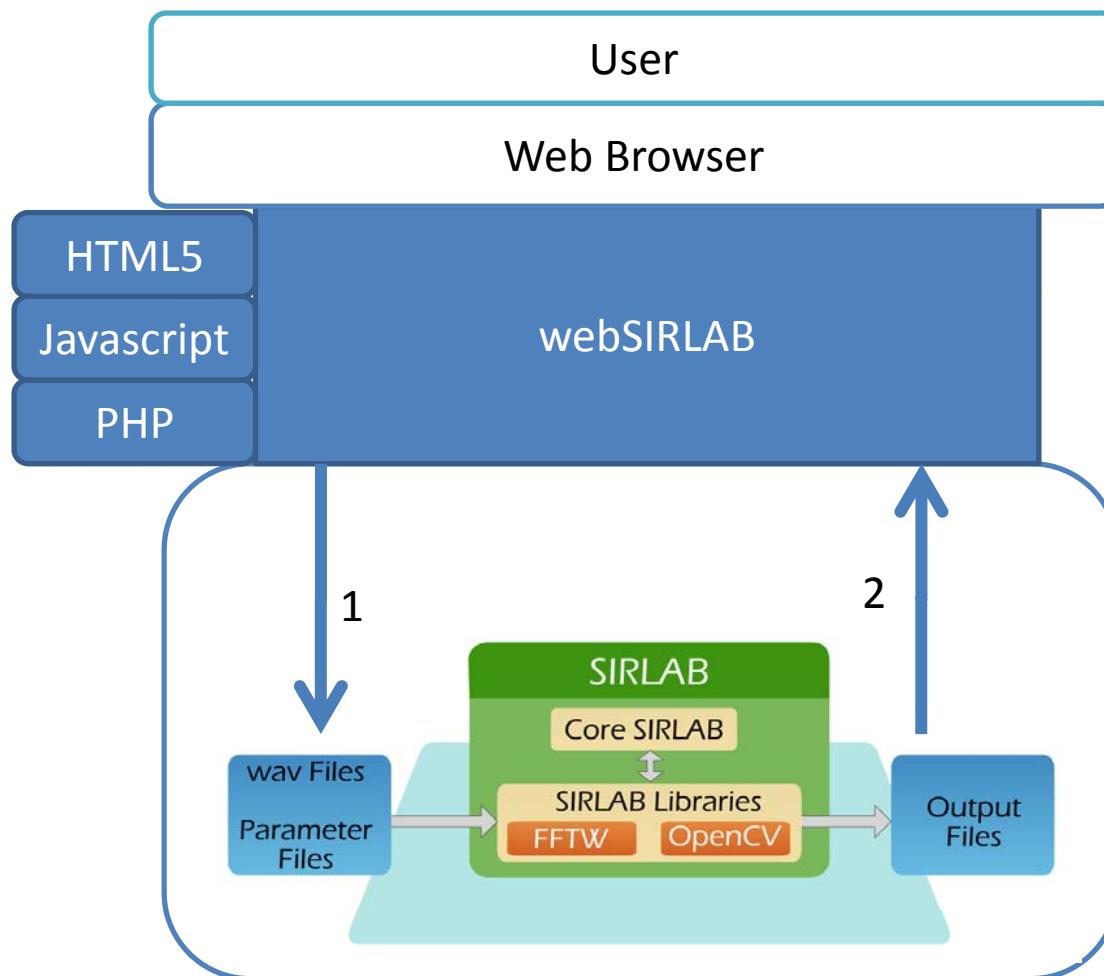
Research contribution

webSIRLAB



Research contribution

webSIRLAB Architecture



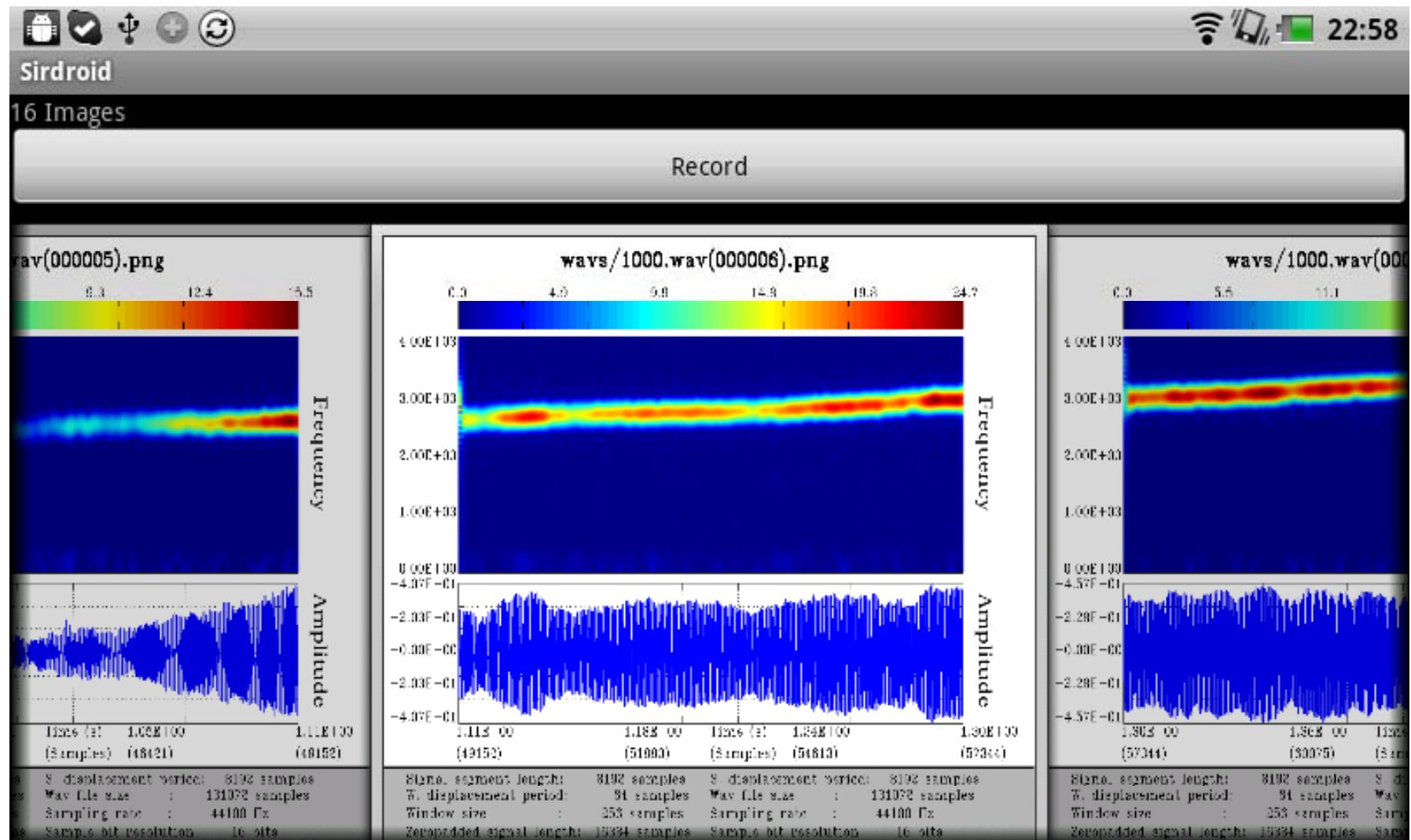
Research contribution

SIRDroid

- Android interface for SIRLAB
 - Android is the leading mobile operating system
- Client Server Architecture
- Can record data on real environment and get results in a few seconds

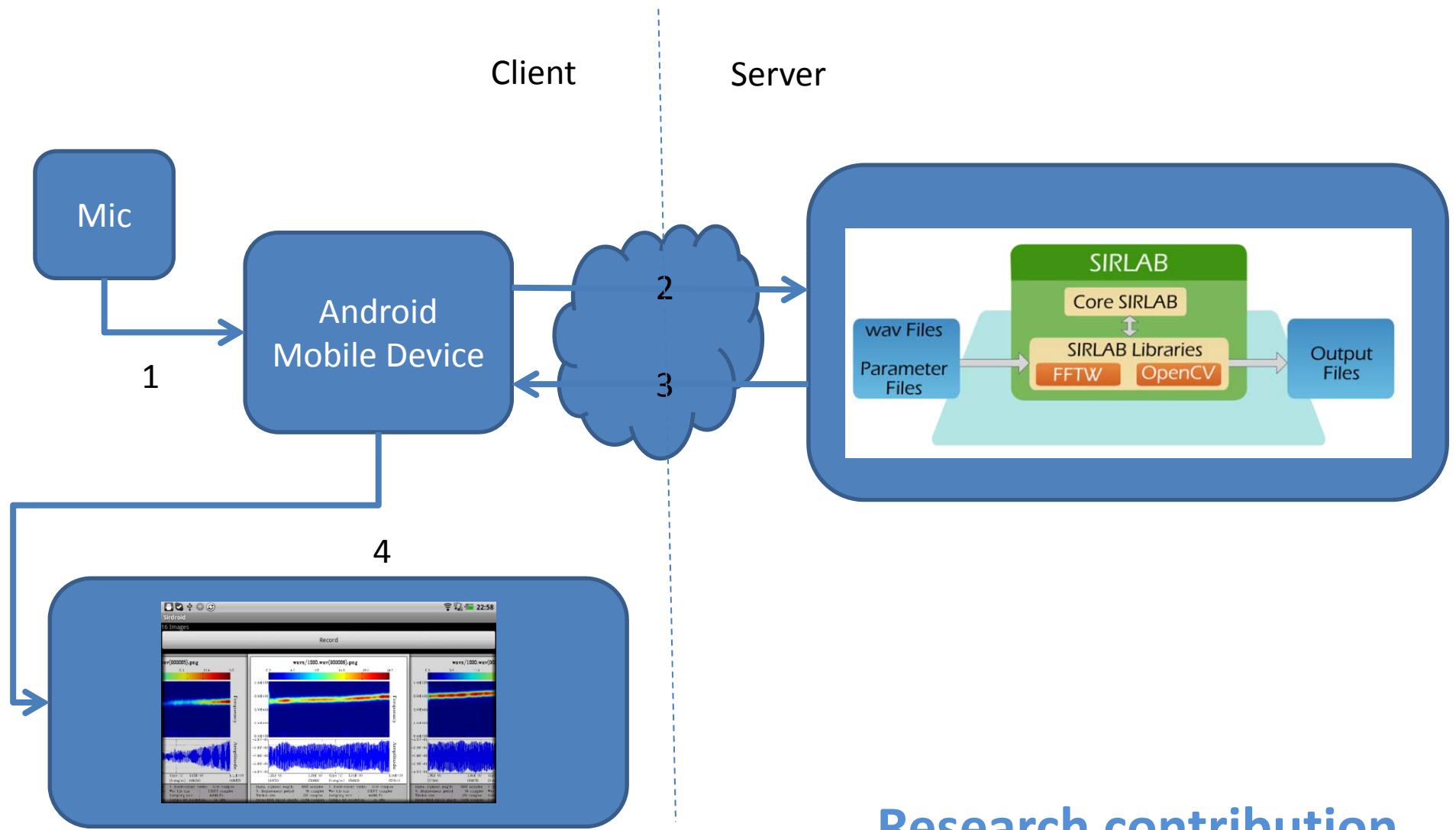
Research contribution

SIRDroid



Research contribution

SIRDroid Architecture

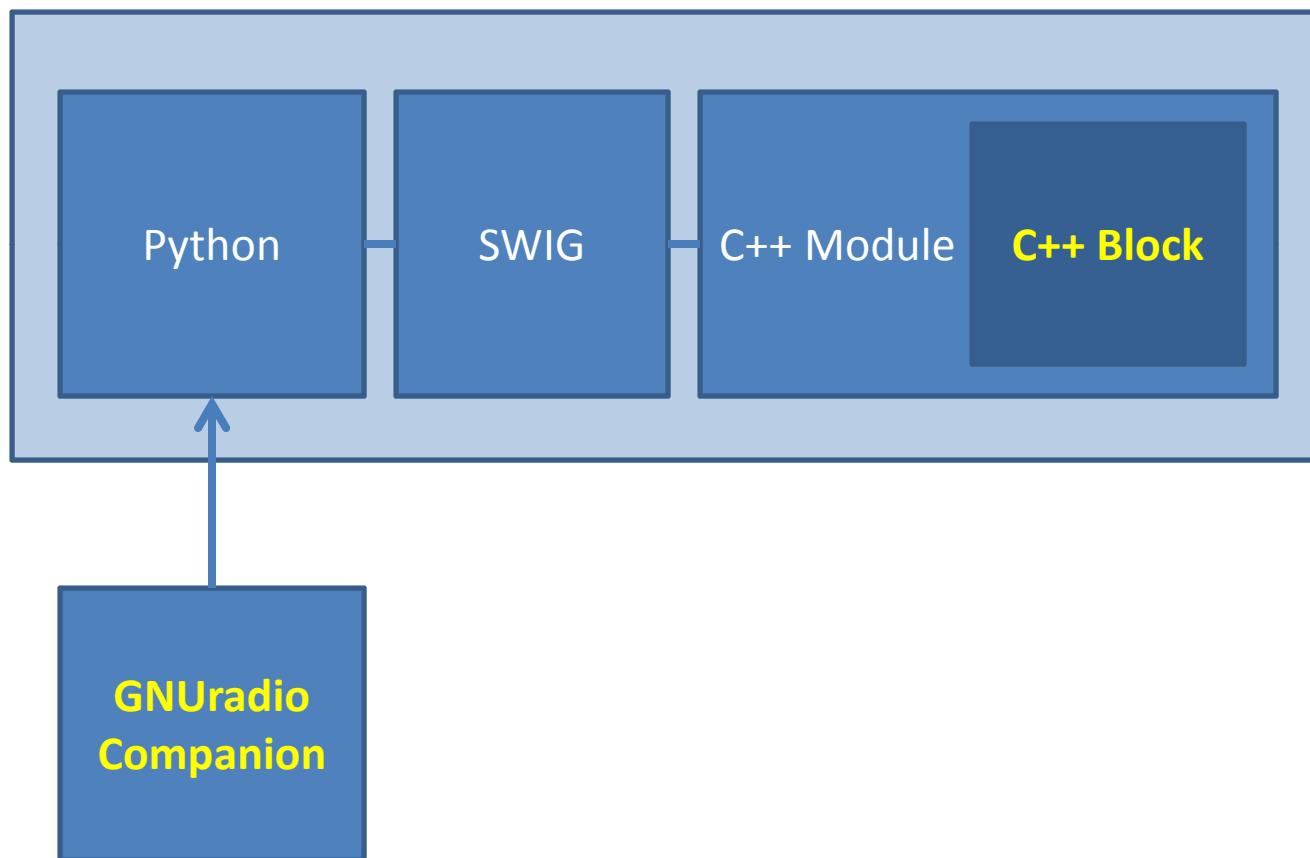


Research contribution

GNURadio

- Open Source Software
- Provides a library of signal processing blocks
- Sends and receives signals
- Audio, USRP, Network (TCP, UDP), File, Wav File
- USRP makes GNURadio wireless capable
- Software Defined Radio

GNURadio Architecture

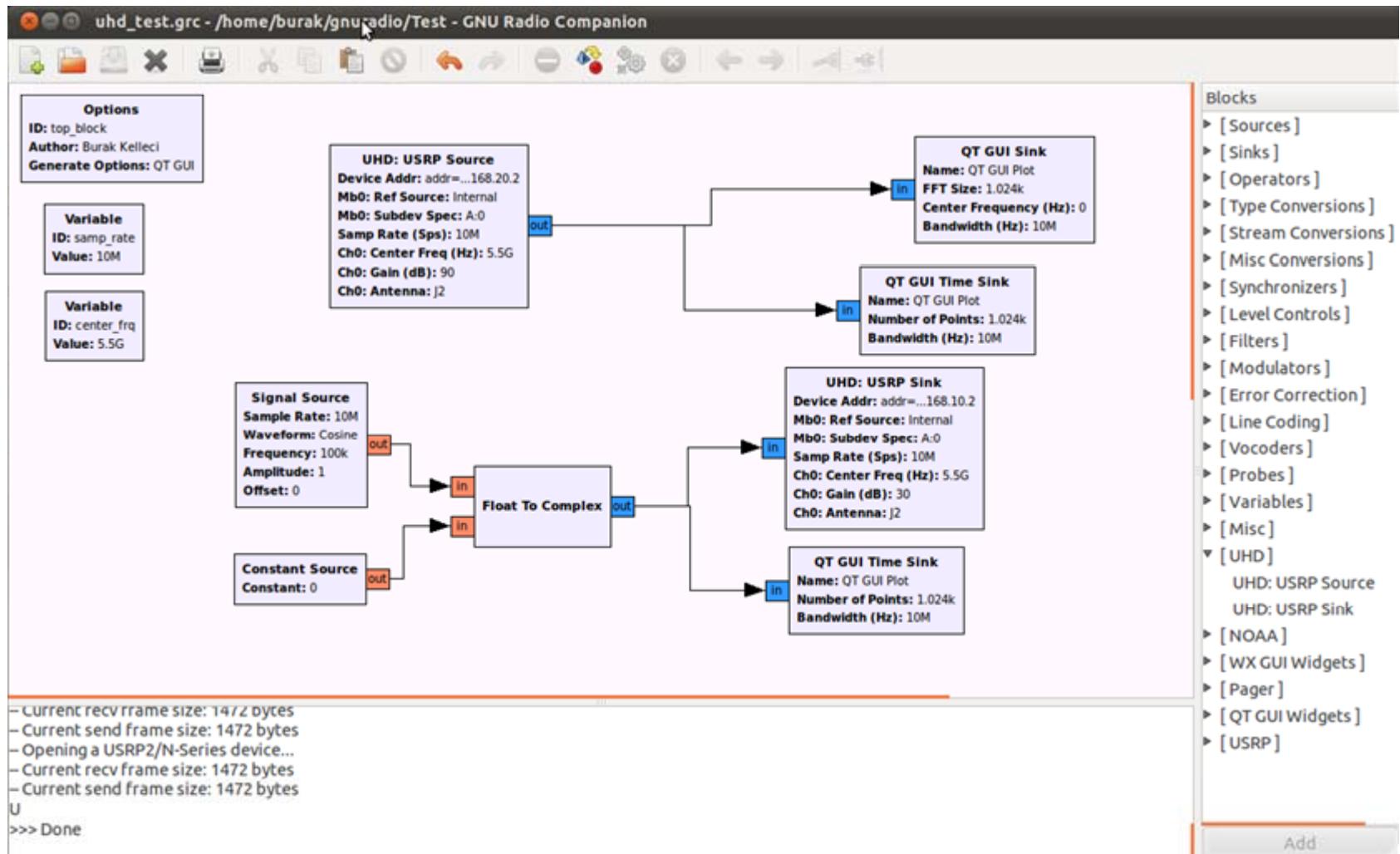


*SWIG: Simplified Wrapper Interface Generator

GNURadio Companion

- Graphical Interface to GNURadio
- Iconic Programming Language
- Powerful Editor
 - Place the Required Blocks
 - Configure Each Block
 - Connect them Together
 - Build and Run

GNUradio Companion



GNURadio Challenges

- Build Time-frequency Representations
 - Short Time Fourier Transform
 - Ambiguity Function
 - Wigner Distribution
 - Choi – Williams Distribution

The theory behind the solution

DESIGN

Design Outline

- Time-Frequency Representations
 - Algorithms, complexity and parallelization
- MIMO Channel
 - MIMO System Modeling
 - Proposed Channel Modeling
 - Modulation-Convolution-Delay
 - Delay-Convolution-Modulation

Time-Frequency Representations

**Short Time Fourier
Transform**

$$S_{x,w}[k, m] = \sum_{n \in \mathbb{Z}_N} x[n]w[n - m]e^{-j2\pi \frac{kn}{N}}$$

**Ambiguity
Function**

$$A_{f,g}[m, k] = \sum_{n \in Z_N} f[n] g^* [\langle n + m \rangle_N] e^{-j2\pi \frac{kn}{N}}$$

**Wigner
Distribution**

$$W_x[n, k] = \frac{1}{N} \sum_{\tau=0}^{N-1} \sum_{v=0}^{N-1} \sum_{l=0}^{N-1} \rho_N e^{j2\pi v l} x[\langle l + \tau \rangle_N] x^*[l] e^{-j\frac{2\pi}{N}(nv + k\tau)}$$

**Choi-Williams
Distribution**

$$C_x[t, f] = \sum_{m=0}^{N-1} \sum_{k=0}^{N-1} A_x[m, k] \Phi[m, k] e^{j\frac{2\pi}{N}(kt - mf)},$$

Short Time Fourier Transform

Algorithm 3 Short Time Fourier Transform

Input: Signal $x[n] \in l^2(\mathbb{Z}_N)$, Window width $w > 0 \in \mathbb{Z}$, Zero-padding $P > 0 \in \mathbb{Z}$.

Output: Matrix $s[M][P]$

```
1:  $M \leftarrow \lfloor \frac{N}{w} \rfloor$ 
2: for  $i = 0 \rightarrow M - 1$  do
3:    $wn \in \mathbb{Z}^N \leftarrow 0$ 
4:    $y \in \mathbb{Z}^P \leftarrow 0$ 
5:   for  $j = 0 \rightarrow w - 1$  do
6:      $wn[j + w \cdot i] \leftarrow 1$ 
7:   end for
8:   for  $j = 0 \rightarrow N - 1$  do
9:      $y[j] \leftarrow x[j] \cdot wn[j]$ 
10:  end for
11:   $s[i] \leftarrow \text{dft}(y)$ 
12: end for
```

Computational Time Complexity: $O(n^2\log(n))$

Research contribution

Ambiguity Function

Algorithm 4 Ambiguity Function

Input: Signal $x[n] \in l^2(\mathbb{Z}_N)$, $y[n] \in l^2(\mathbb{Z}_N)$

Output: Matrix $A[N][N]$

```
1: for  $i = 0 \rightarrow N - 1$  do
2:   for  $j = 0 \rightarrow N - 1$  do
3:      $y1[j] \leftarrow \text{conj}(y[\text{mod}(j + i, N)])$ 
4:   end for
5:   for  $j = 0 \rightarrow N - 1$  do
6:      $z[j] \leftarrow x[j] \cdot y1[j]$ 
7:   end for
8:    $A[i] \leftarrow \text{dft}(z)$ 
9: end for
```

Computational Time Complexity: $O(n^2\log(n))$

Research contribution

Wigner Distribution

Algorithm 5 Wigner

Input: Signal $x[n] \in l^2(\mathbb{Z}_N)$, $y[n] \in l^2(\mathbb{Z}_N)$

Output: Matrix $W[N][N]$

```
1: for  $i = 0 \rightarrow N - 1$  do
2:   for  $j = 0 \rightarrow N - 1$  do
3:      $y1[j] \leftarrow \text{conj}(y[\text{mod}(j + i, N)])$ 
4:   end for
5:   for  $j = 0 \rightarrow N - 1$  do
6:      $z[j] \leftarrow x[j] \cdot y1[j]$ 
7:   end for
8:    $A[i] \leftarrow \text{dft}(z)$ 
9: end for
10:  $W \leftarrow \text{dft2}(A)$ 
```

Computational Time Complexity: $O(n^2\log(n))$

Research contribution

Choi-Williams Distribution

Algorithm 6 Choi-Williams

Input: Signal $x[n] \in l^2(\mathbb{Z}_N)$, $y[n] \in l^2(\mathbb{Z}_N)$, α

Output: Matrix $W[N][N]$

```
1: for  $i = 0 \rightarrow N - 1$  do
2:   for  $j = 0 \rightarrow N - 1$  do
3:      $y1[j] \leftarrow y[\text{mod}(j + i, N)]$ 
4:   end for
5:   for  $j = 0 \rightarrow N - 1$  do
6:      $z[j] \leftarrow x[j] \cdot y1[j]$ 
7:   end for
8:    $A[i] \leftarrow \text{dft}(z)$ 
9:   for  $j = 0 \rightarrow N - 1$  do
10:     $A[i][j] \leftarrow A[i][j] \cdot e^{-\alpha(i \cdot j)^2}$ 
11:  end for
12: end for
13:  $W1 \leftarrow \text{dft2}(A)$ 
14:  $W \leftarrow \text{conj}(W1)$ 
```

Computational Time Complexity: $O(n^2 \log(n))$ **Research contribution**

MIMO System

The channel is seen as a linear system

$$\textcolor{brown}{y} = Hx + N.$$

H then is decomposed

$$H = \textcolor{brown}{U}\Sigma V^*$$

Finally

$$\textcolor{brown}{U}^{-1}y = \Sigma(V^*x) + \textcolor{brown}{N}$$

The symbols are preprocessed at the transmitter and post-processed at the receiver

MIMO System

- The channel must be estimated
 - Several mechanisms have been proposed and implemented
 - Subject to errors
- The Shannon capacity increases linearly with every pair of antennas at the transmitter and receiver.

Formulated MIMO Channel

- A “MxN” MIMO channel can be seen as a collection of $C=MxN$ Single Input Single Output (SISO) Channels.
- Every SISO Channel is then modeled like a channel with 3 operators:
 - **Delay:** The signal has a latency while is propagating
 - **Convolution:** The medium acts like a FIR Filter
 - **Modulation:** The medium inserts a Doppler shift
- The order is important, this yields two approximations:
 - Delay-Convolution-Modulation (DCM)
 - Modulation-Convolution-Delay (MCD)

Research contribution

DCM

Operators

$$y_{a,b} = g_{a,b} \odot_D X_{k_{a,b}},$$

where $g_{a,b} \in l^2(\mathbb{Z}_D)$

$$g_{a,b} = T_{h_{a,b}}\{f_{a,b}\},$$

where $f_{a,b} \in l^2(\mathbb{Z}_D)$

$$f_{a,b} = x_b \circledast_D \delta_{m_{a,b}}.$$

Composition

$$y_{a,b} = (T_{h_{a,b}}\{x_b \circledast_D \delta_{m_{a,b}}\}) \odot_D X_{k_{a,b}}.$$

MIMO

$$y_a = \sum_{b=0}^{M-1} (T_{h_{a,b}}\{x_b \circledast_D \delta_{m_{a,b}}\}) \odot_D X_{k_{a,b}}.$$

Research contribution

MCD

$$y_{a,b} = g_{a,b} \circledast_D \delta_{m_{a,b}},$$

Operators

where $g_{a,b} \in l^2(\mathbb{Z}_D)$

$$g_{a,b} = T_{h_{a,b}}\{f_{a,b}\},$$

where $f_{a,b} \in l^2(\mathbb{Z}_D)$

$$f_{a,b} = x_b \odot_D X_{k_{a,b}}.$$

Composition

$$y_{a,b} = (T_{h_{a,b}}\{x_b \odot_D X_{k_{a,b}}\}) \circledast_D \delta_{m_{a,b}}.$$

MIMO

$$y_a = \sum_{b=0}^{M-1} (T_{h_{a,b}}\{x_b \odot_D X_{k_{a,b}}\}) \circledast_D \delta_{m_{a,b}},$$

Research contribution

The code behind the solution

IMPLEMENTATION

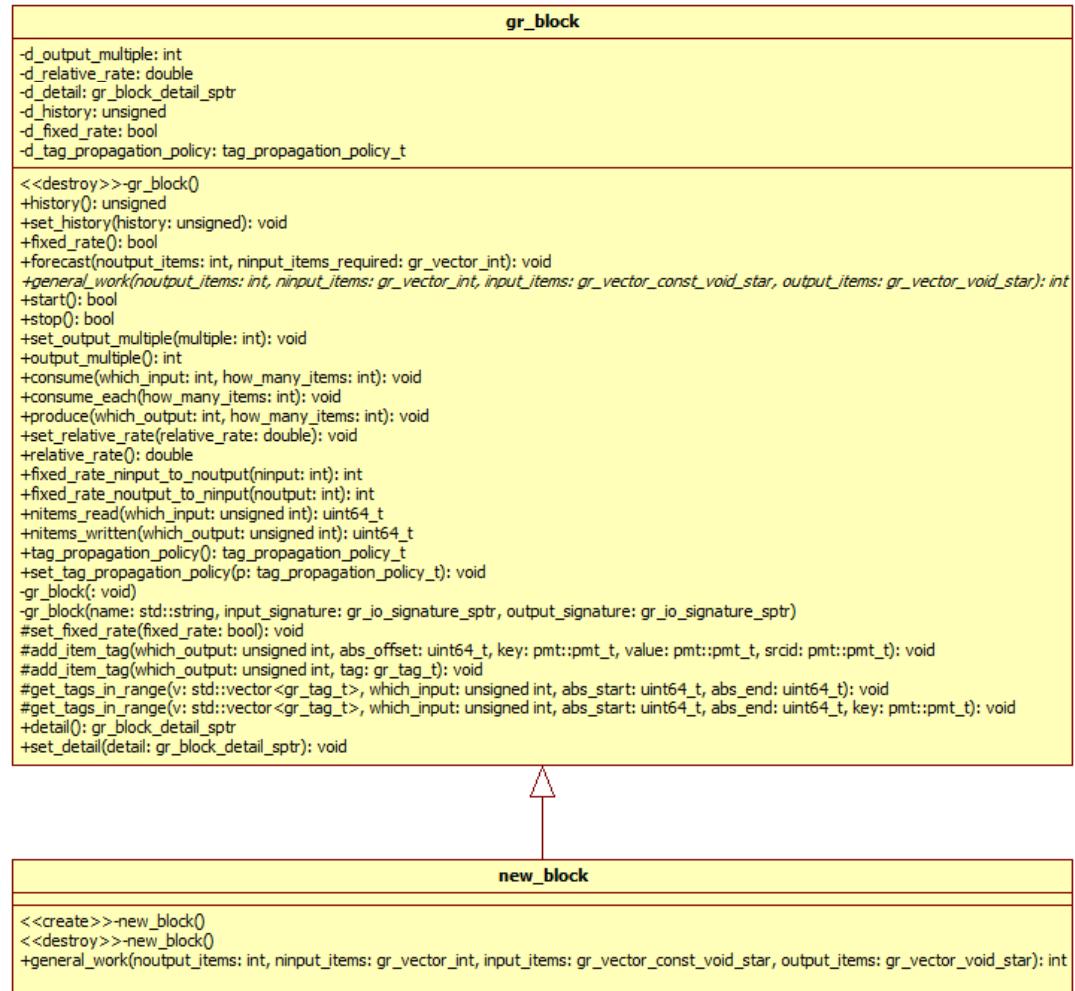
Time Frequency Representations

- The main implementation is done in C++
- Object oriented programming
- Each time-frequency representation is a class
 - Implements from *gr_block* interface
 - The method *general_work* is implemented
 - A constructor sets the initial properties of each time frequency representation

Time-Frequency Representations

Block
Interface

Constructor,
destructor and
general_work are
implemented



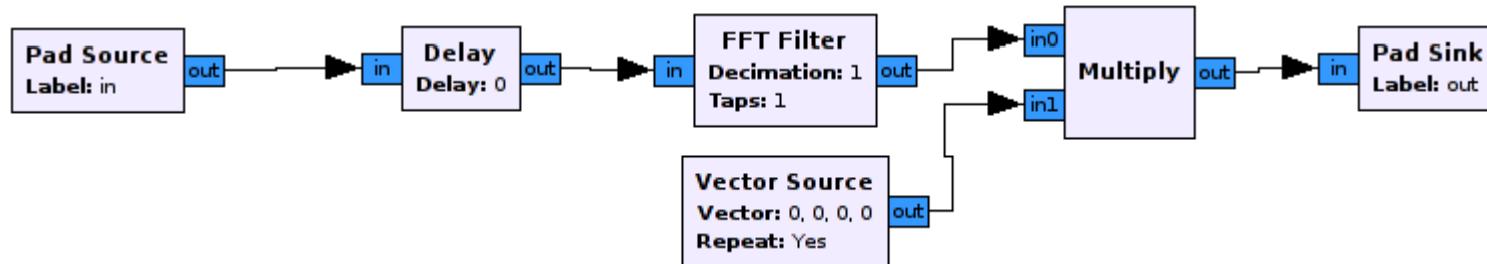
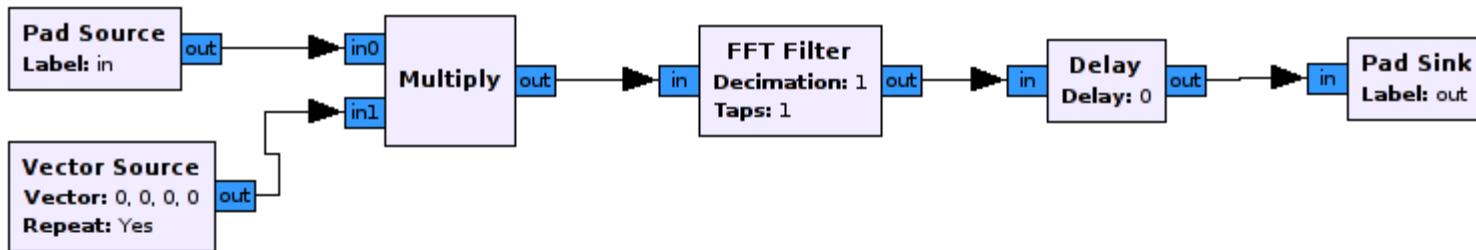
Parallelization

- Each running block is a thread into the whole system
- Our time-frequency representation blocks are executed in parallel as an option
 - Data parallelism
 - OpenMP was selected for parallelization
 - API for automatic parallelization, include compiler directives, libraries and functions
 - Cross compatibility, great support and meets the project requirement

MIMO Channel

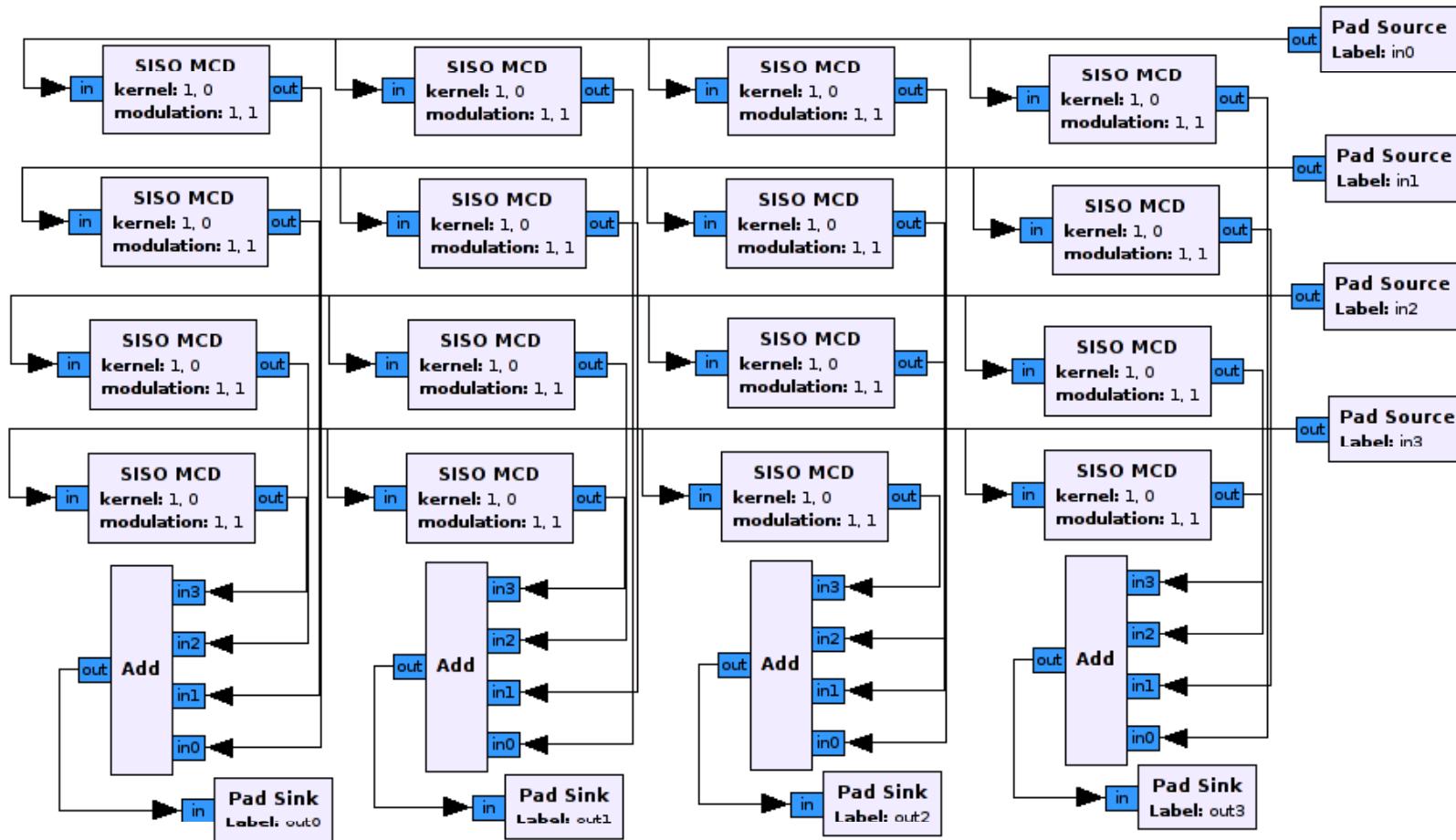
- Development of each block, MCD and DCM internally with GNUradio Companion
- Iconic Programming

MCD and DCM Blocks



Research contribution

4x4 MIMO



Research contribution

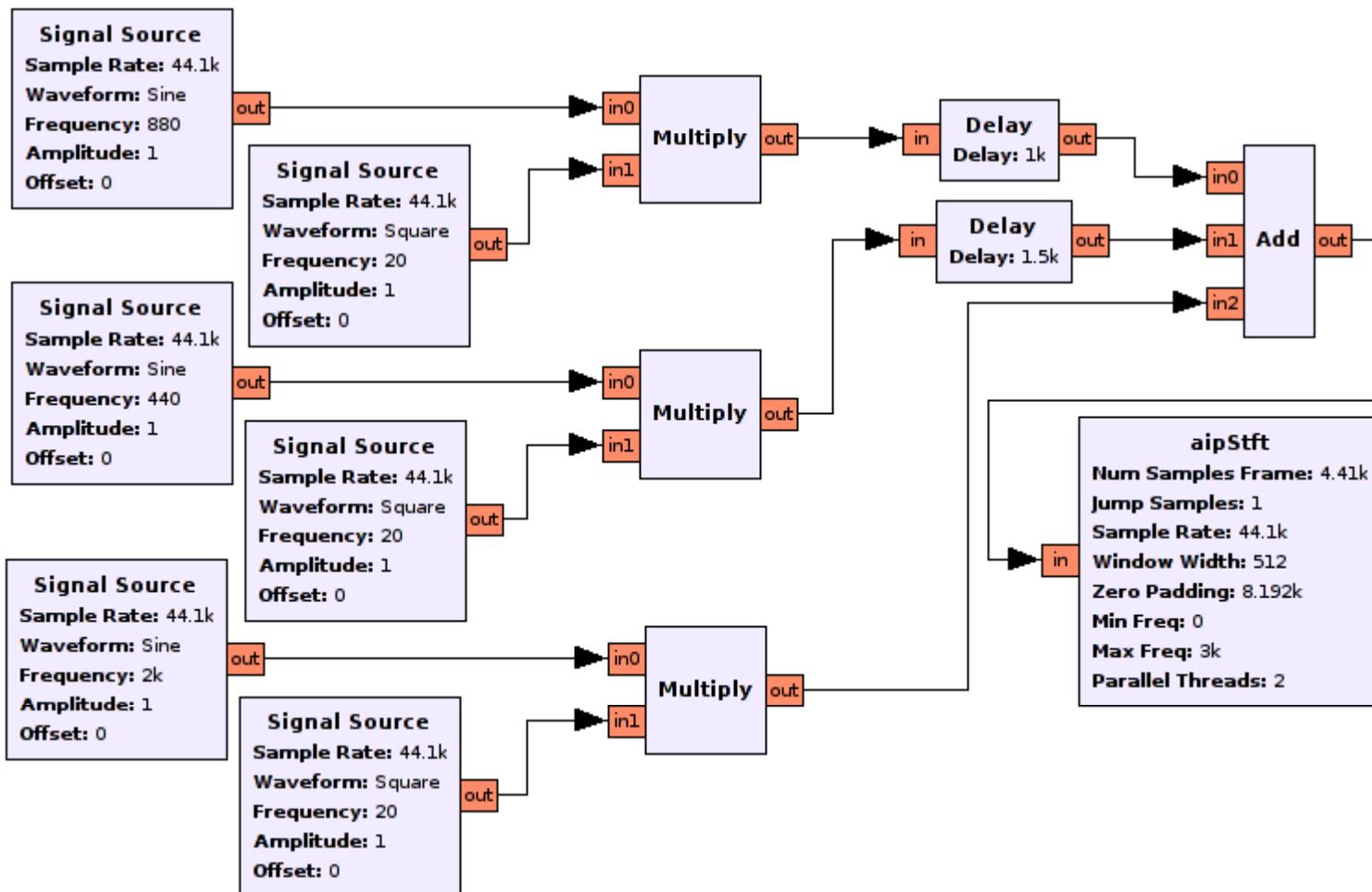
The results behind the solution

TESTING

Acoustic Channel Surveillance

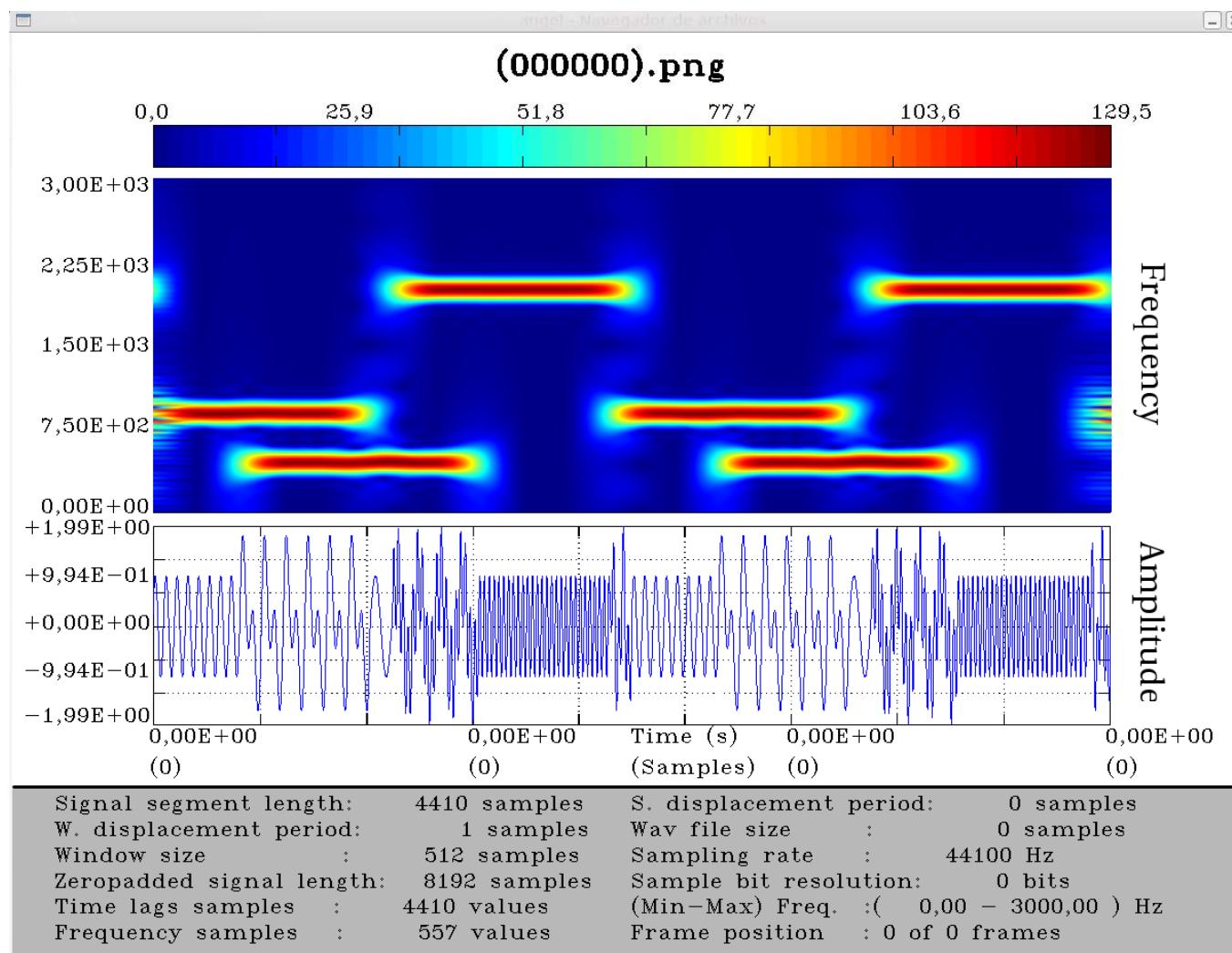
- The STFT can be used to monitor the environment
 - Species characterization in bioacoustics
 - Sonar

Acoustic Channel Surveillance



Research contribution

Channel Surveillance

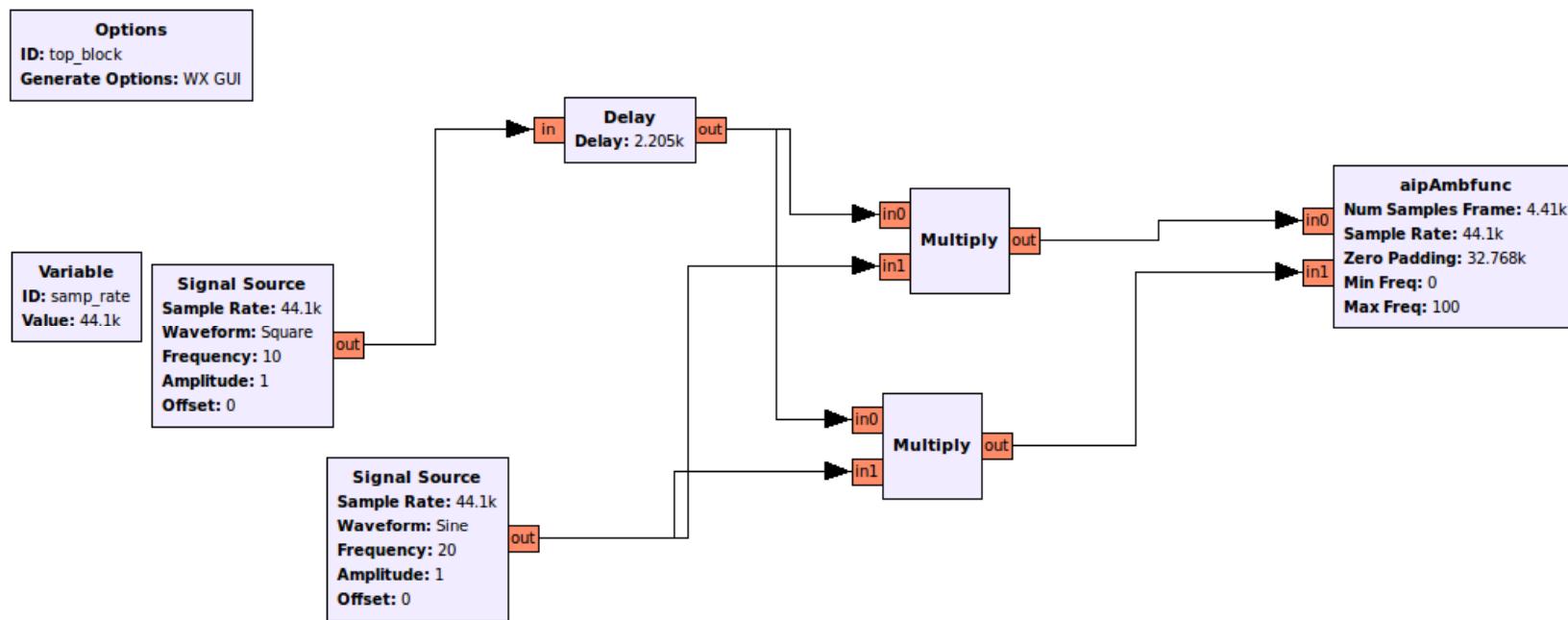


Research contribution

Ambiguity Function

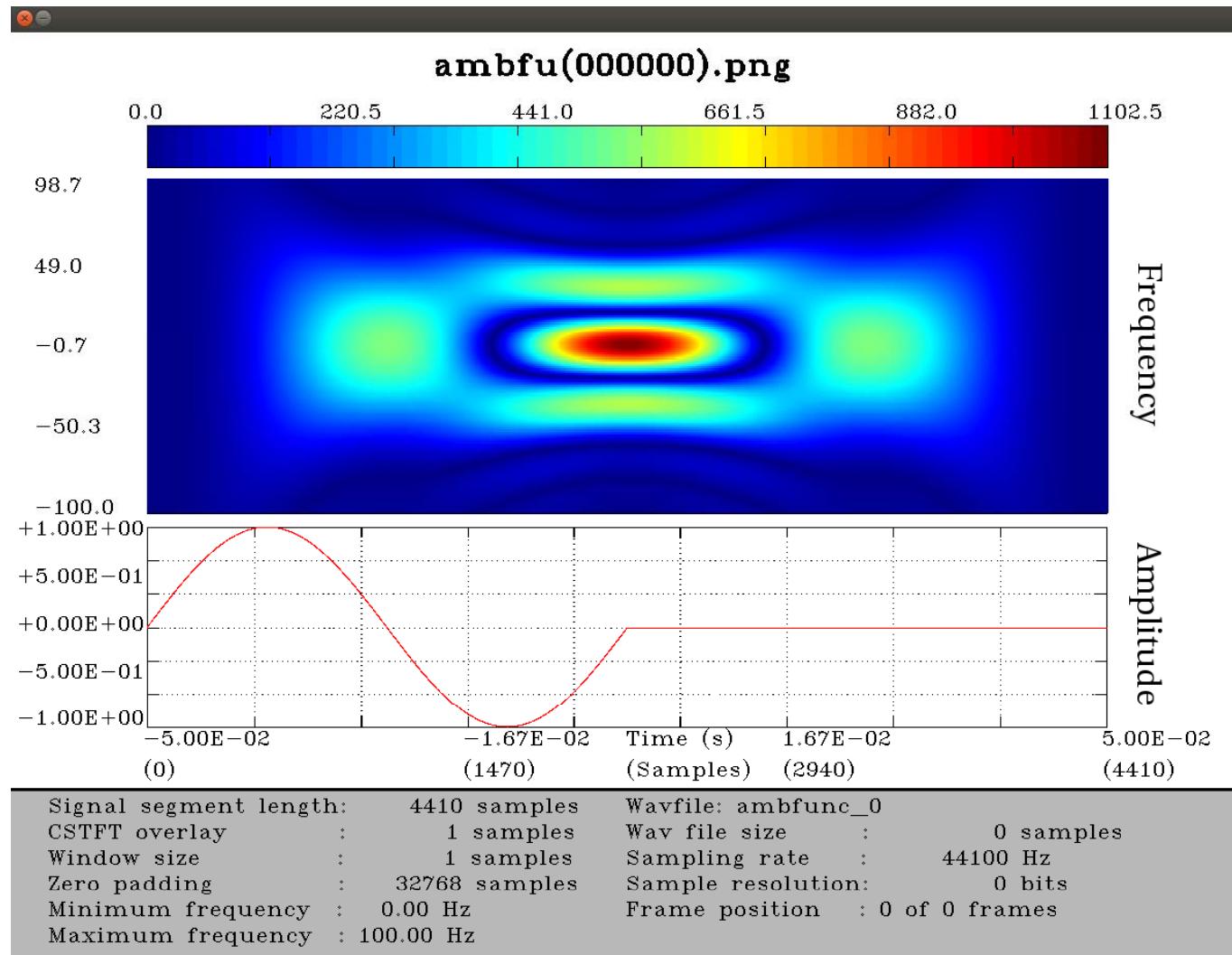
- Used for Sonars
- Design of Signals
- Detection of Delay and Doppler Shifts
- Testing With Well Known Signals
 - Sine
 - Square

Sine



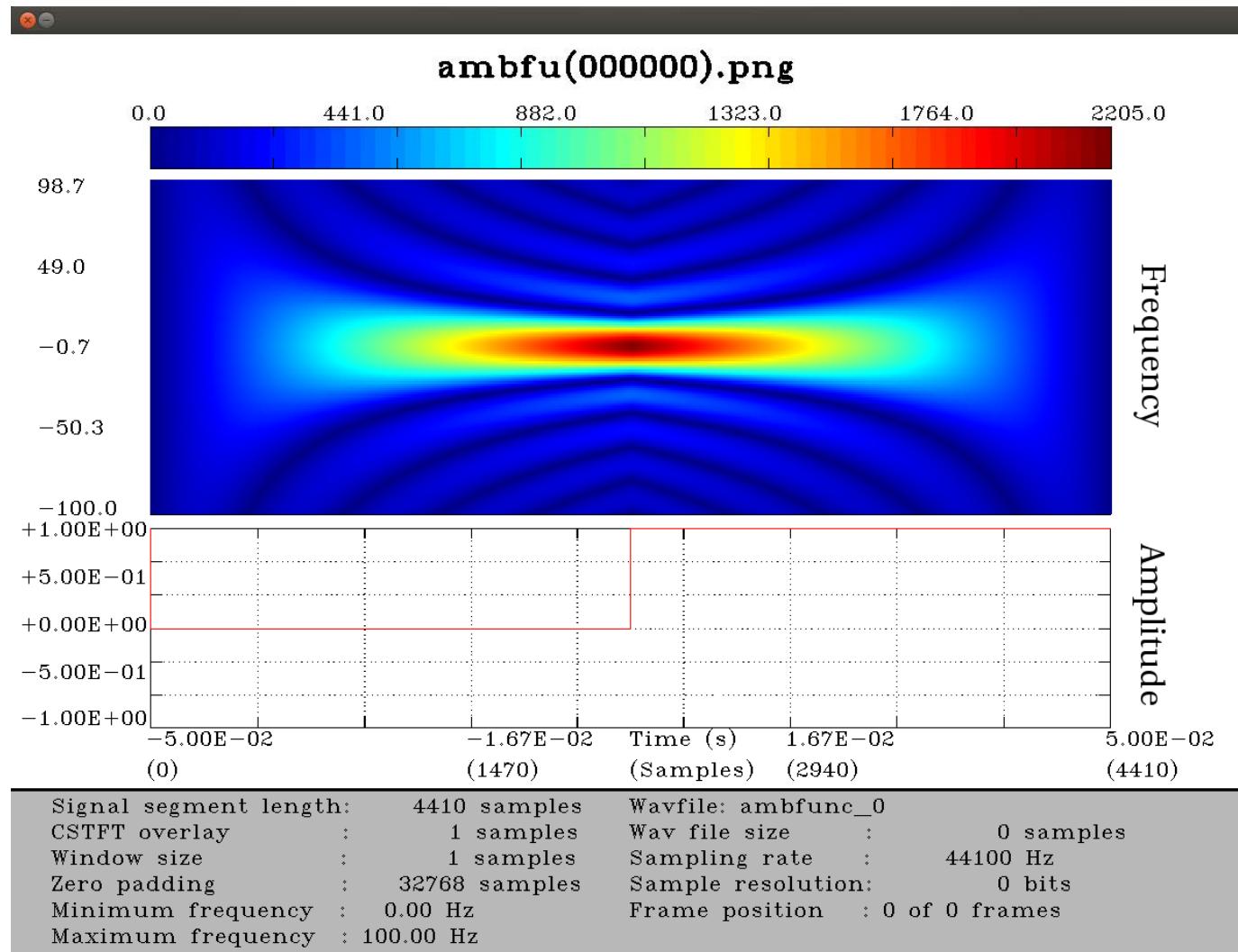
Research contribution

Sine



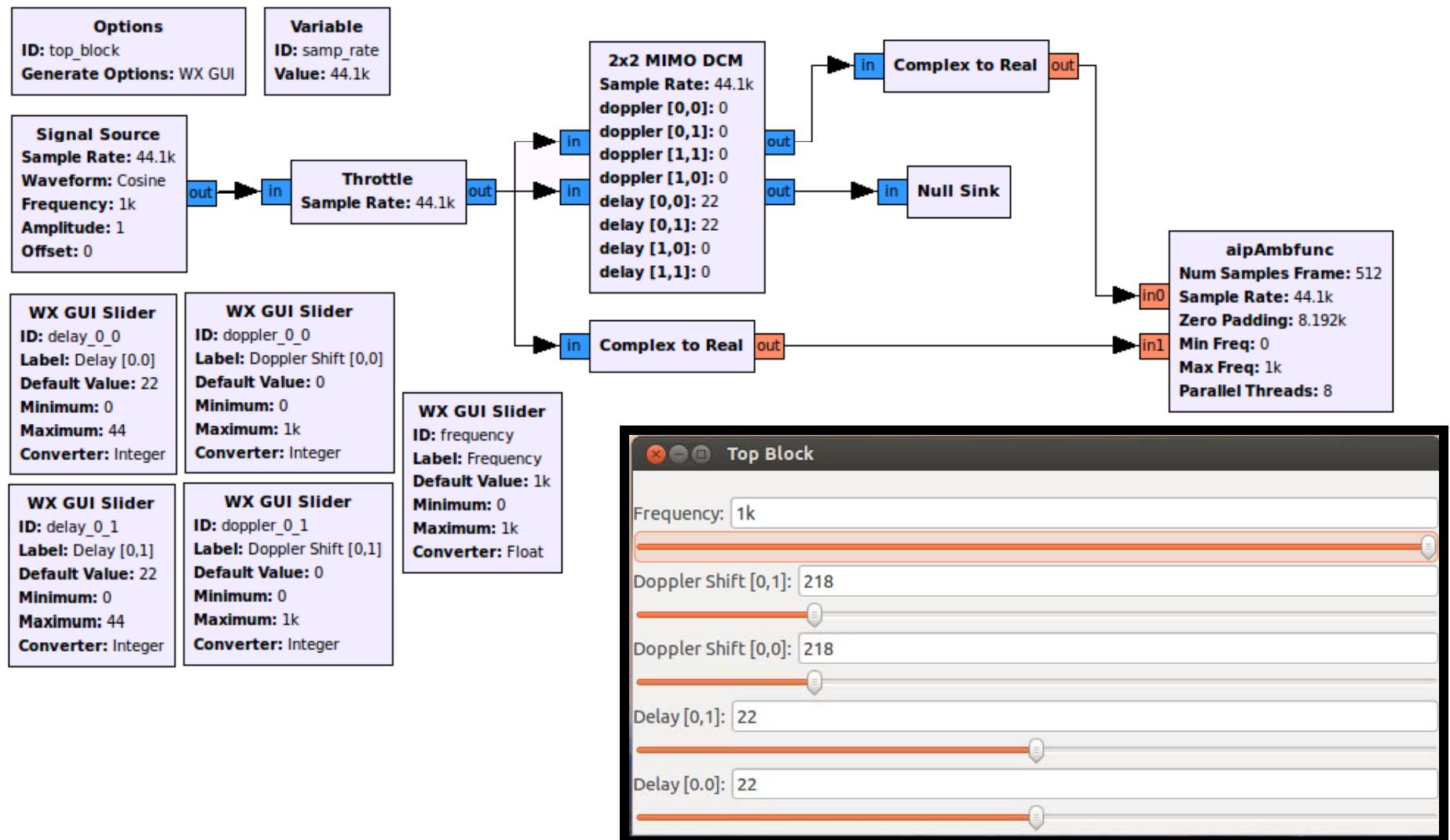
Research contribution

Square



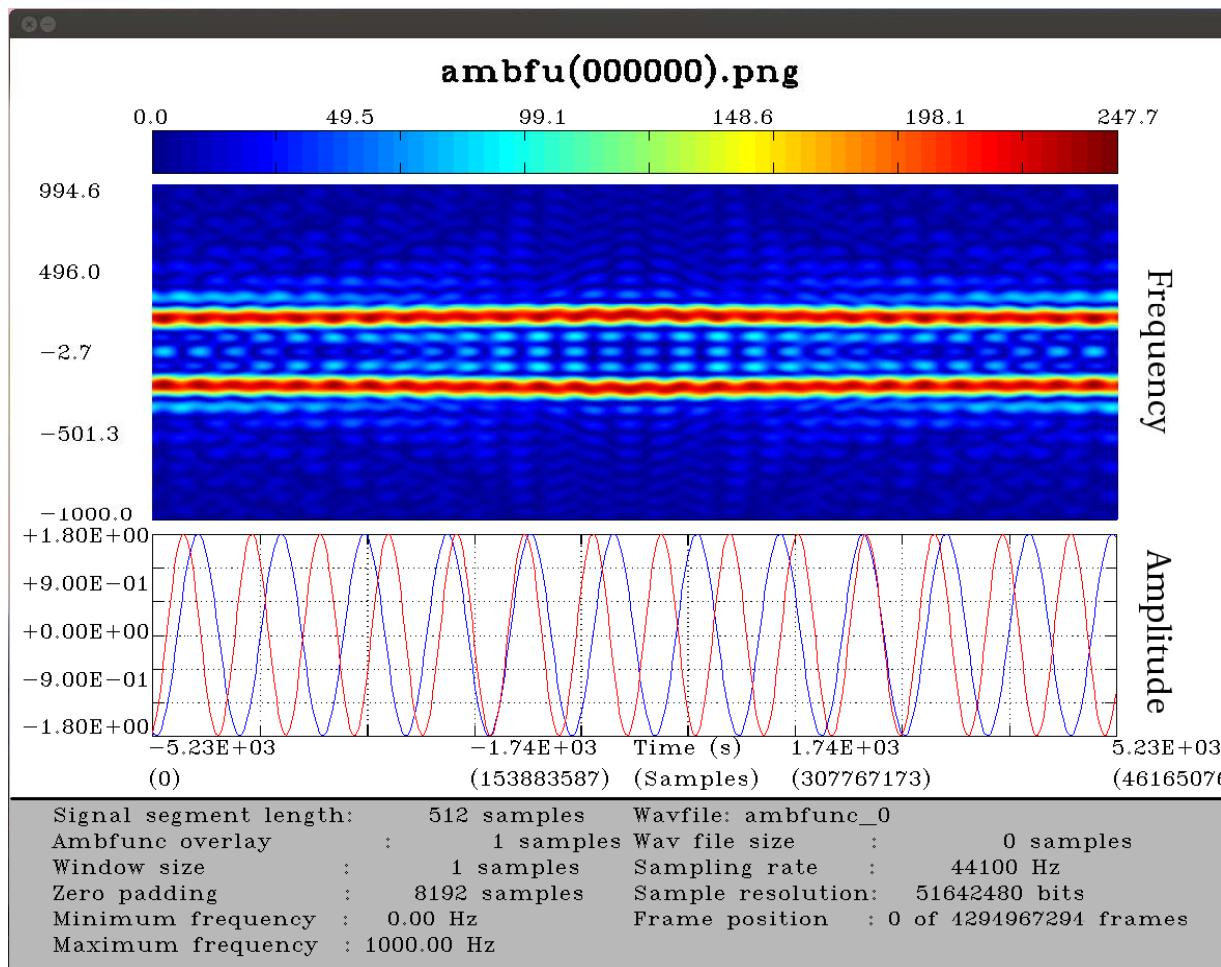
Research contribution

2x2 MIMO



Research contribution

2x2 MIMO

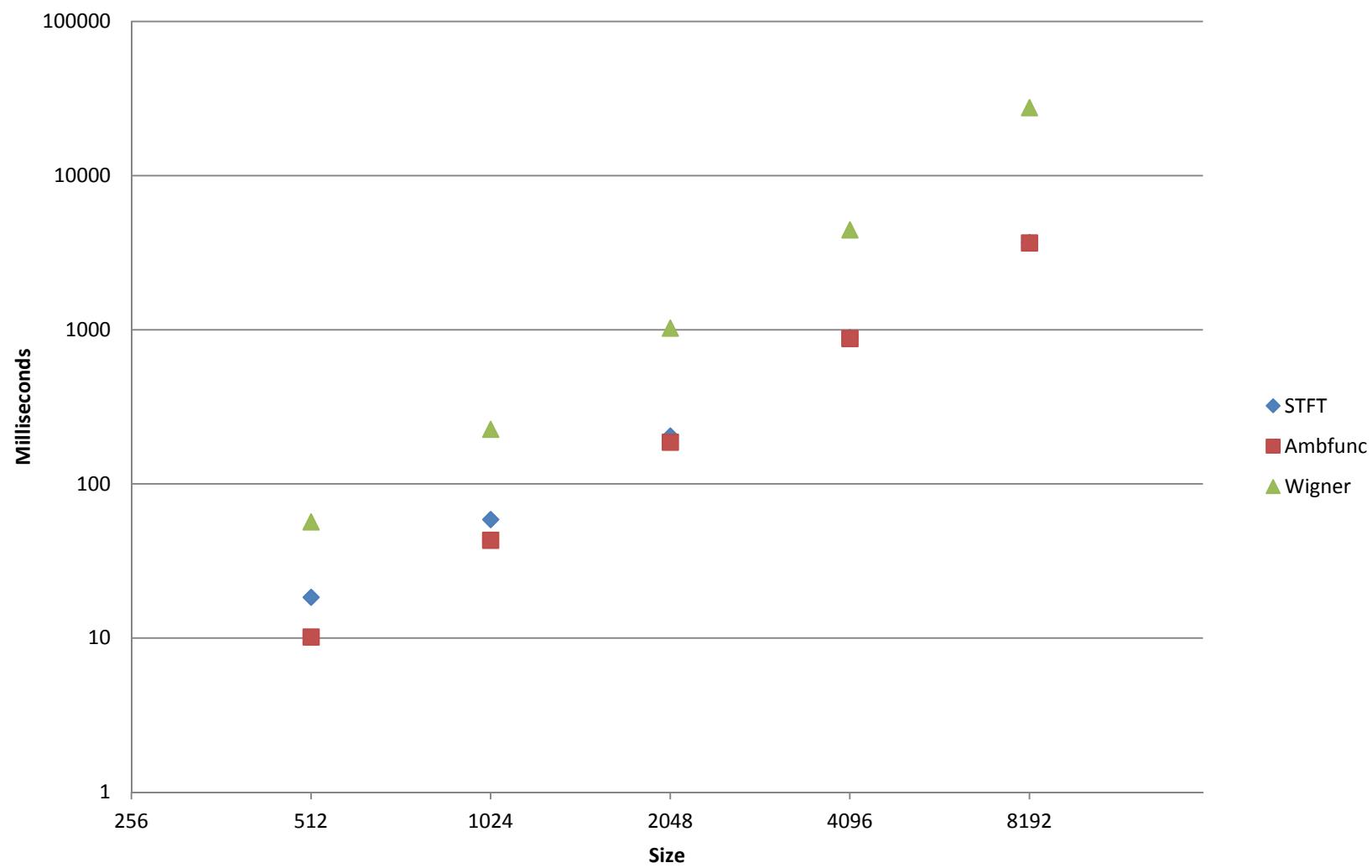


Research contribution

Parallelization Metrics

- Dell 1520
- Intel Core2 T5850
 - 2.16 GHz
 - 4MB Cache
 - 2 Cores, 2 Threads
- 4GB@667MHz
- Linux 2.32
- Samsung RC512
- Intel Core i7 2630QM
 - 2.0 -> 2.9 GHz
 - 6MB Cache
 - 4Cores, 8 Threads
- 6GB@1333MHz
- Linux 3.2

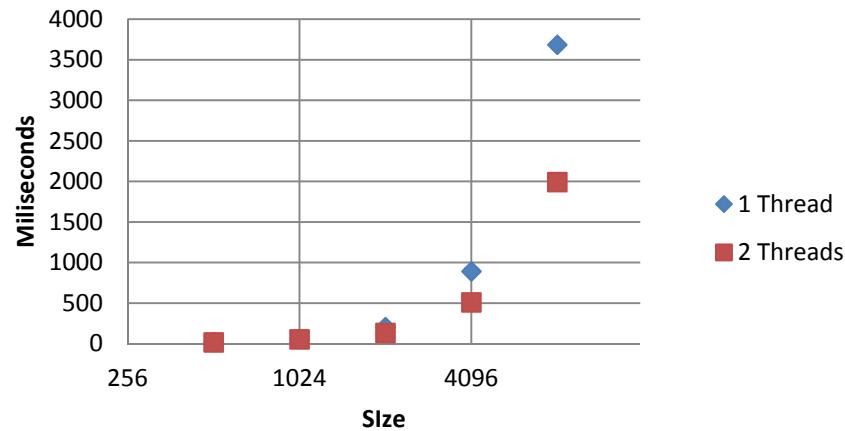
Dell 1520



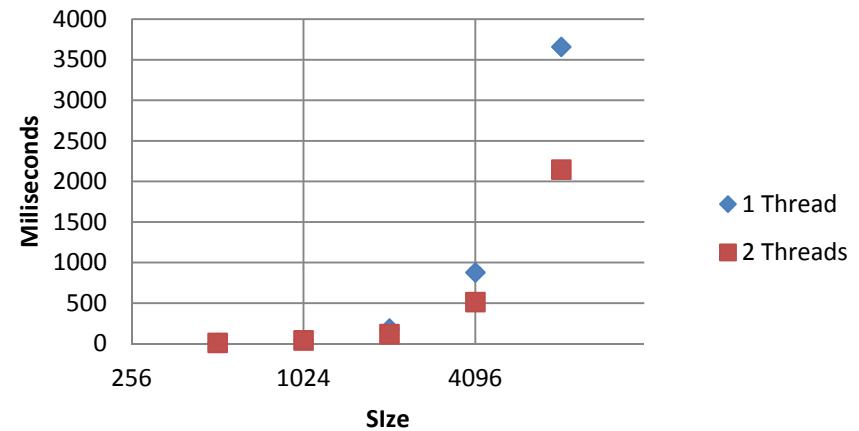
Research contribution

Dell 1520

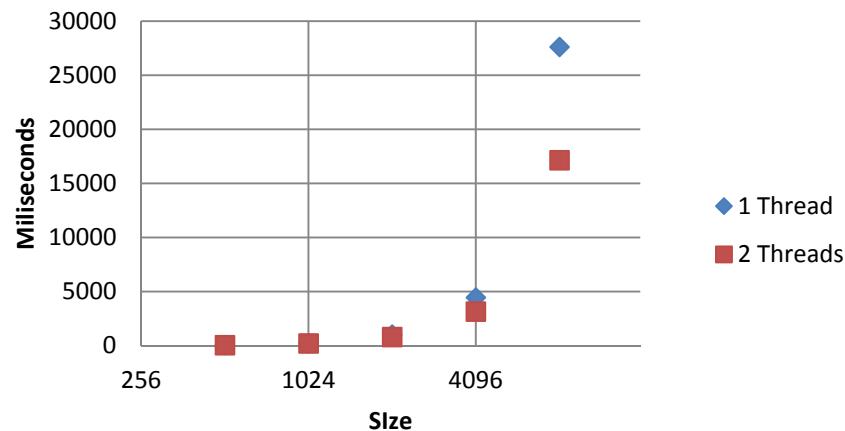
STFT



AmbFunc



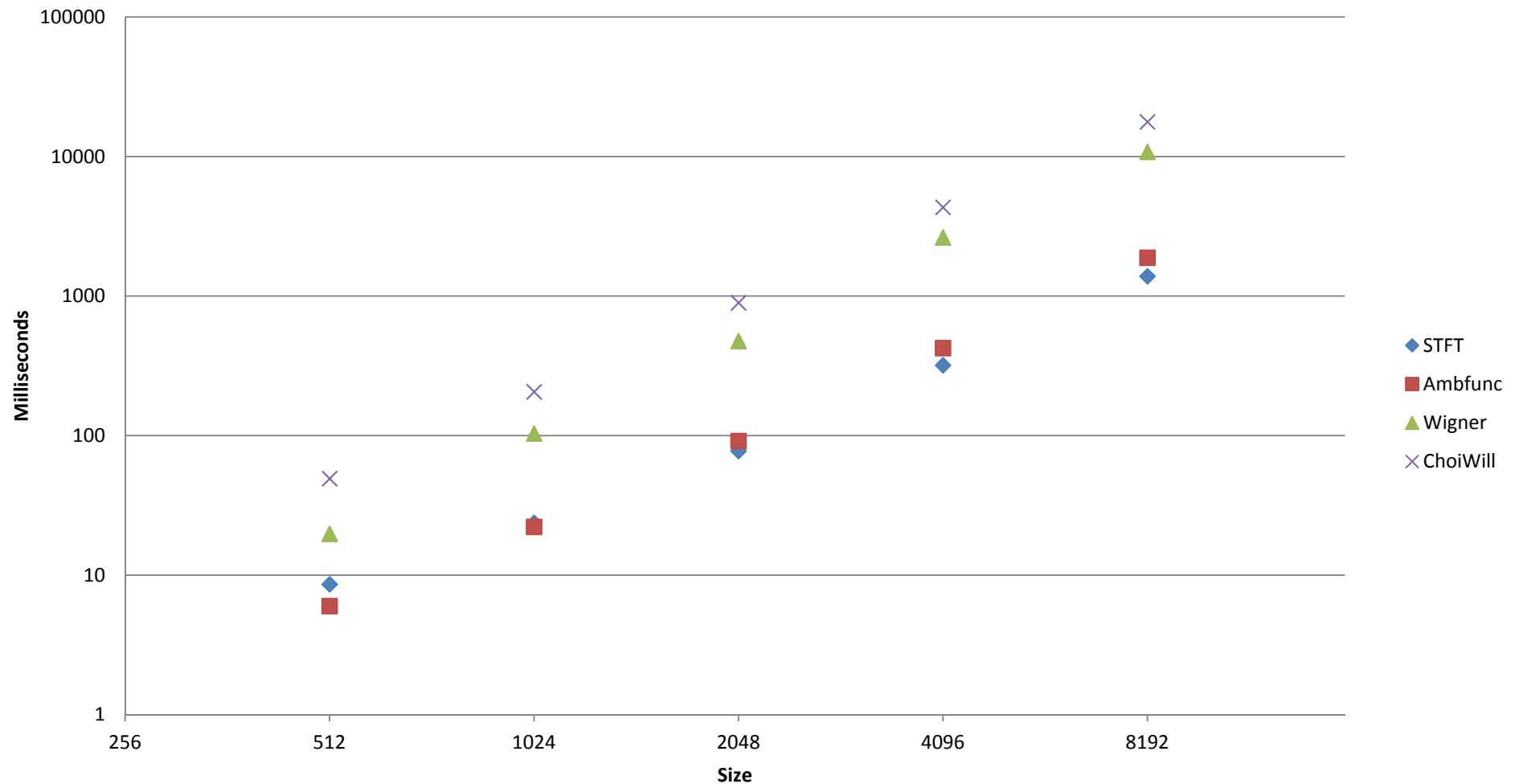
Wigner



Research contribution

Samsung RC512

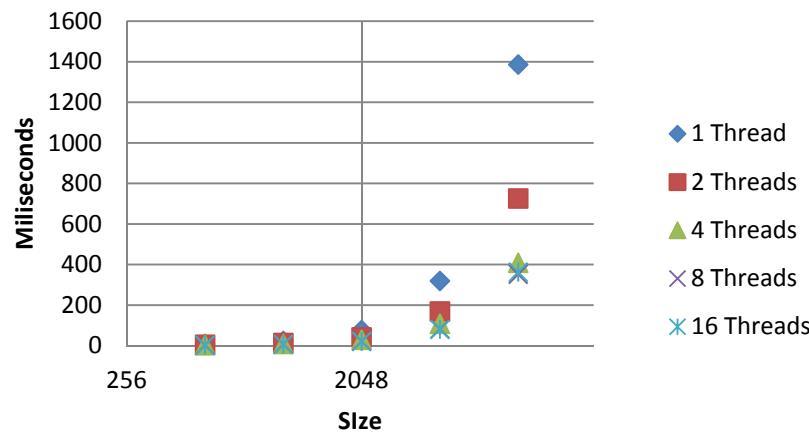
Time-Frequency Representations



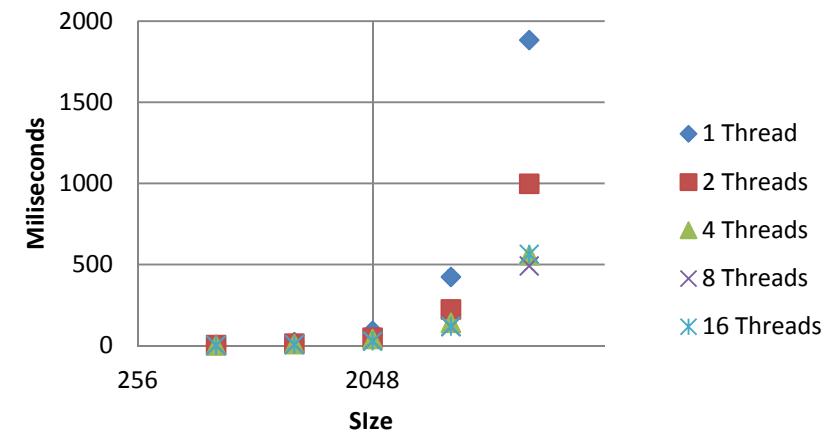
Research contribution

Samsung RC512

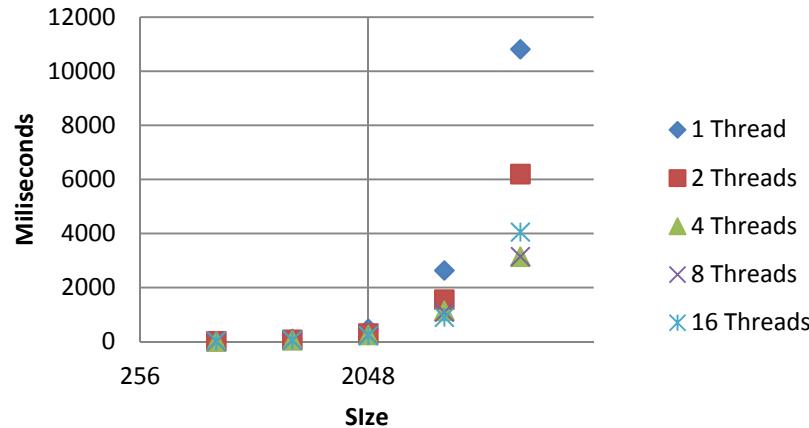
STFT



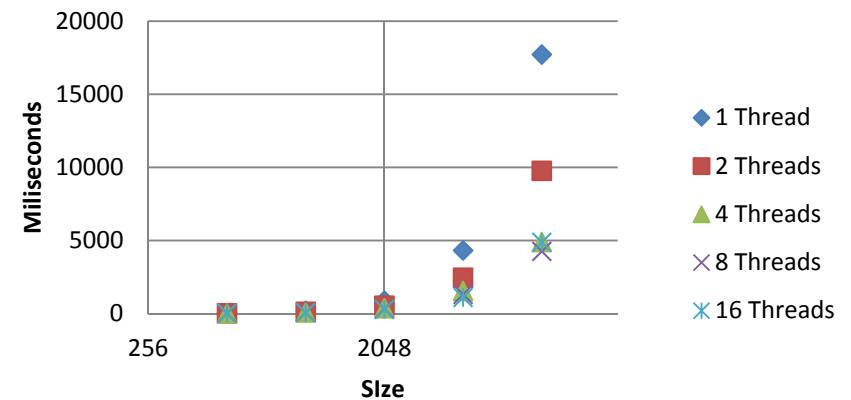
AmbFunc



Wigner



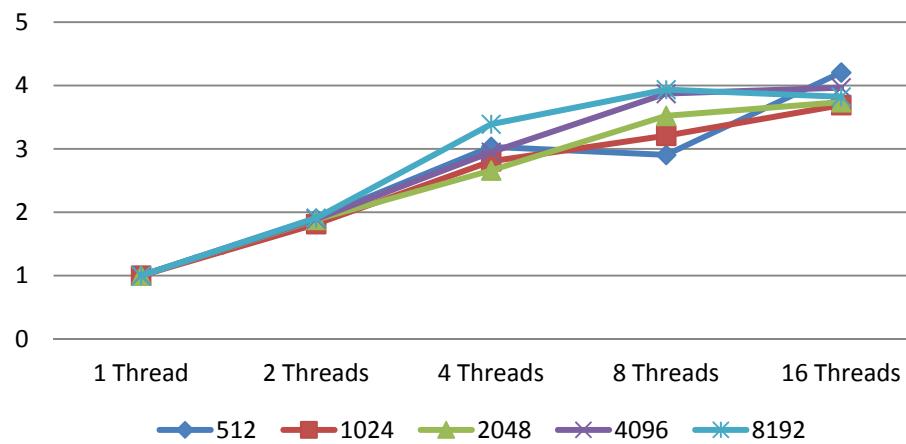
ChoiWill



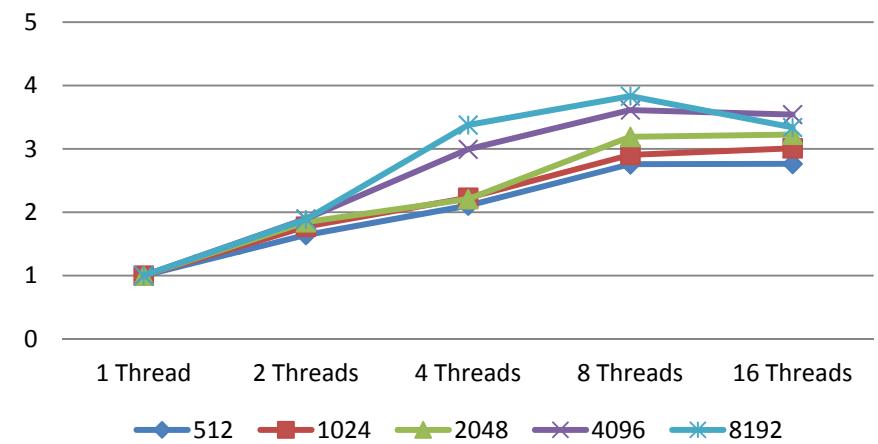
Research contribution

Speed Ups

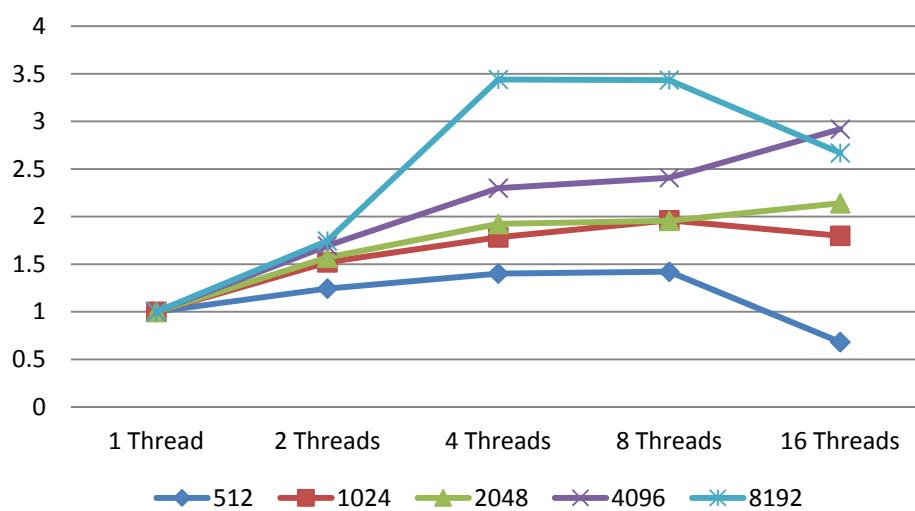
Speed Up STFT



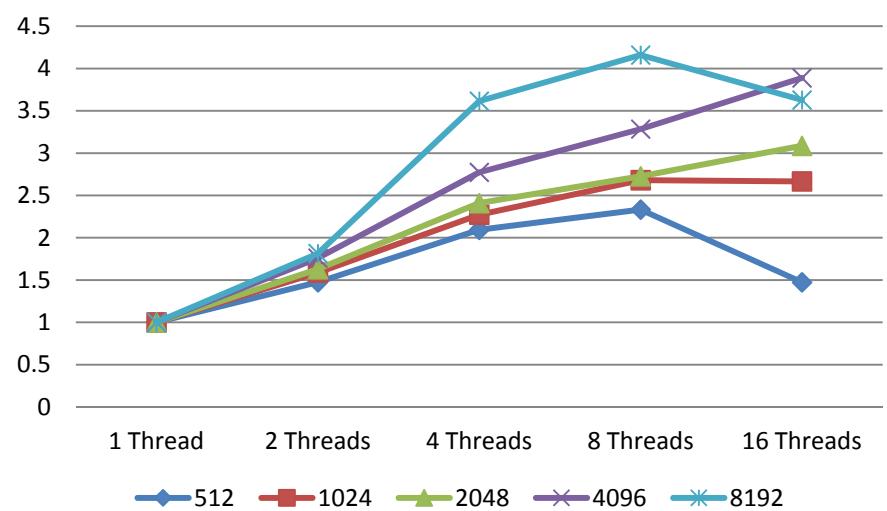
Speed Up AmbFunc



Speed Up Wigner



Speed Up ChoiWill



Conclusions

- A MIMO Modeling framework was presented using a software defined radio paradigm into GNUradio.
- Several time-frequency blocks were designed into GNUradio using the proposed framework.
- A testing workflow was defined using the models and algorithms developed.
- Several works requiring a time-frequency representation can take advantage of the developed framework.

Contributions

- MIMO Channel Modeling
- SIRLAB Web Integration
- SIRLAB Android Integration
- STFT, AmbFunc, Wigner, Choi-Williams SDR Implementation
- MIMO Channel SDR Implementation
- Applications: Channel Surveillance
- Publications:
 - IEEE LASCAS
 - IBERSENSOR

Future work

- Channel Estimation
- Develop Input Signals With the Framework
- DSP, FPGA Integration
- *NetSig Integration*